

Neutrino Factory Physics

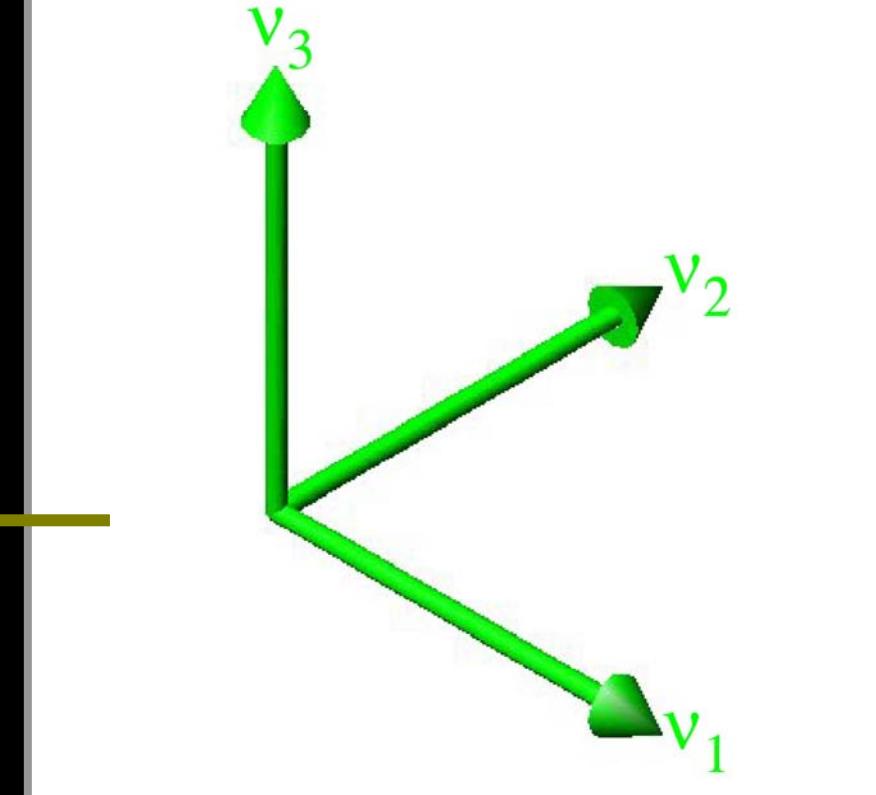
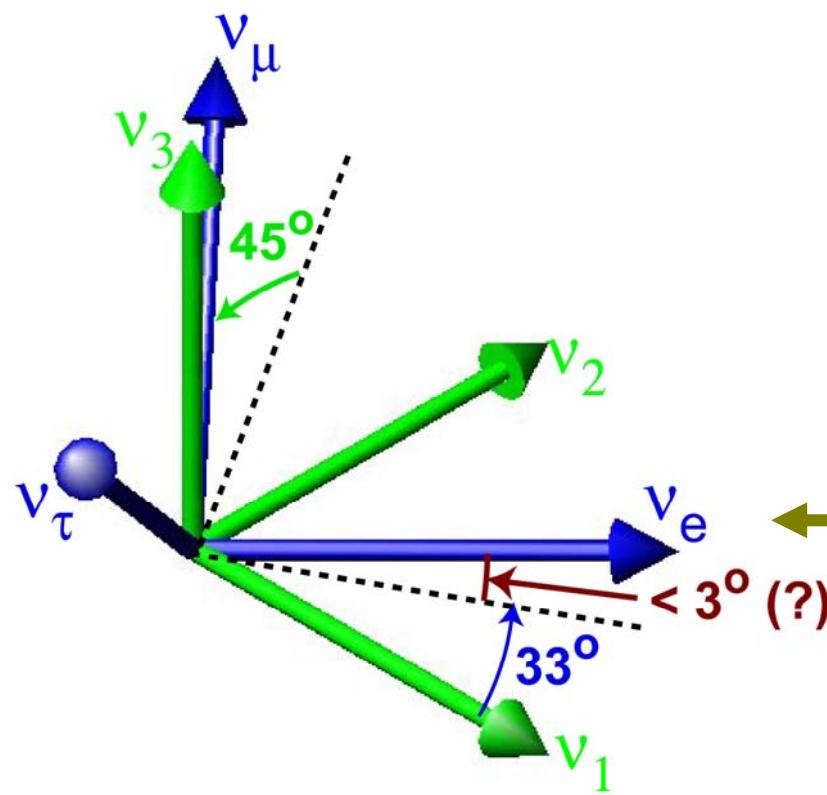
– headline tour

Contents

- Motivation
- Neutrino Factory concept
- Sensitivity
- Conclusions

Motivation: phenomenology

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



Motivation: phenomenology

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} =$$

Solar

eric

$$\begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

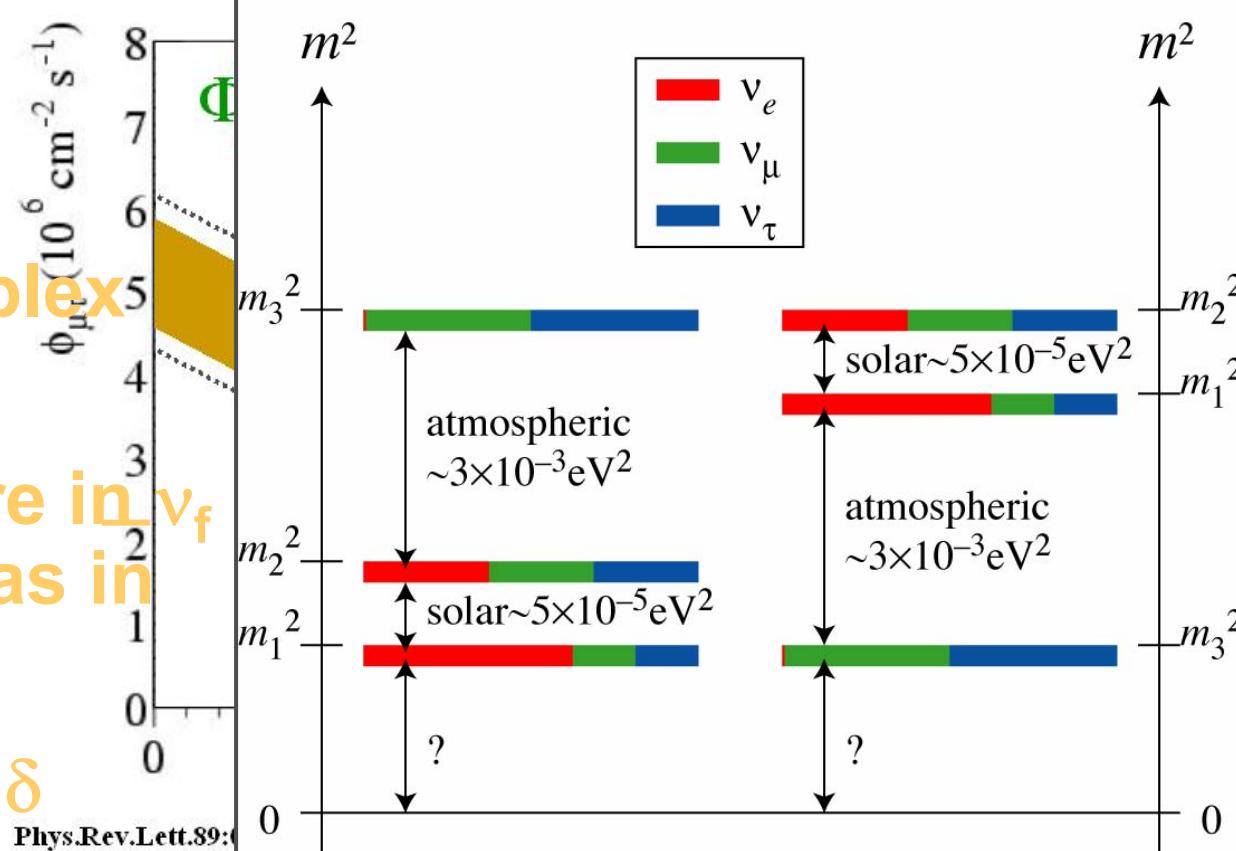
■ CP violation

→ $\nu_f \rightarrow \bar{\nu}_f$

→ Involves complex conjugation

→ Result: mixture in ν_f not the same as in $\bar{\nu}_f$

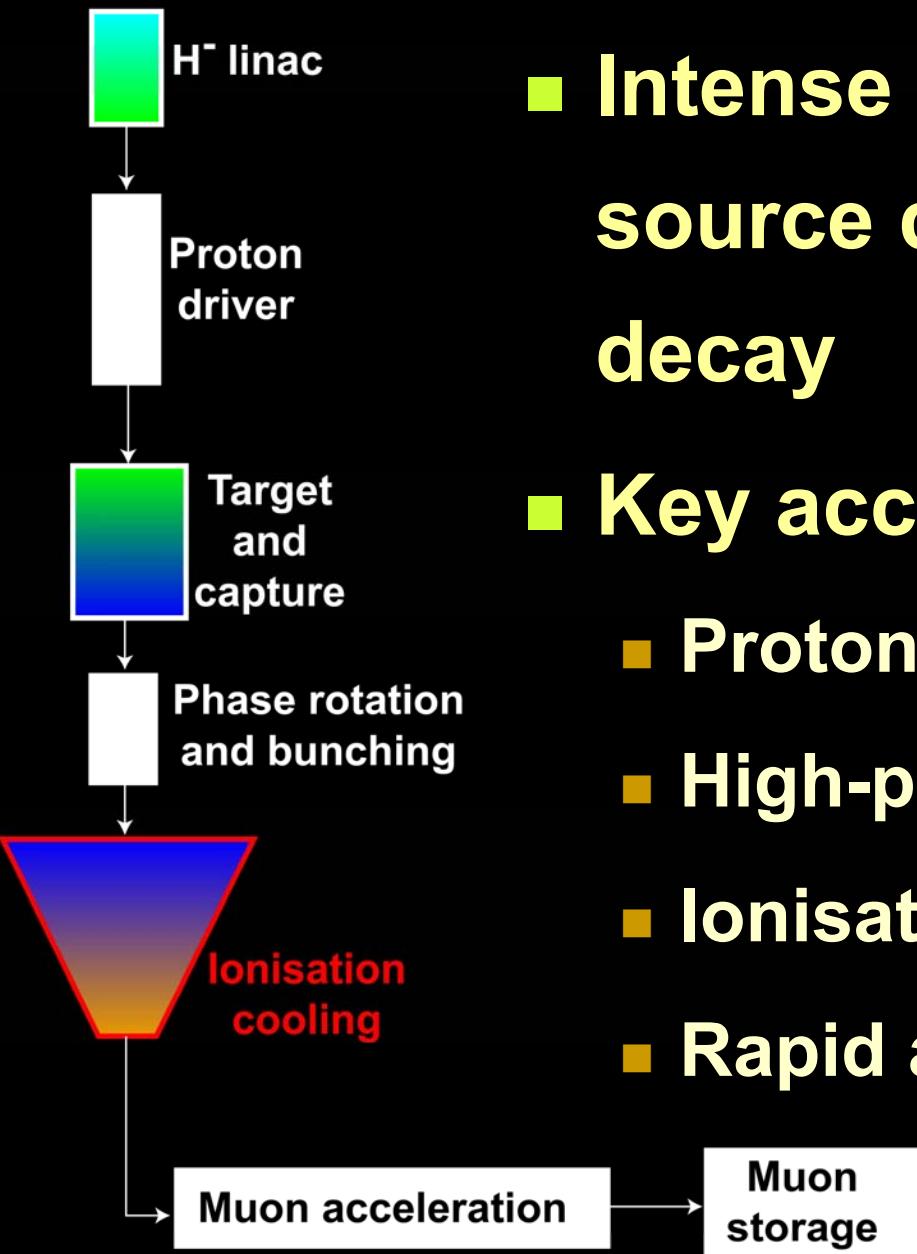
→ Controlled by δ



Motivation: parameters

- Mixing of three flavours of Dirac neutrino:
 - Three mixing angles: θ_{23} , θ_{12} , θ_{13}
 - CP phase: δ
 - Mass differences: Δm^2_{23} , Δm^2_{12}
- Two more CP phases for Majorana neutrino:
 - Oscillation insensitive to Majorana phases
- Neutrino Factory for *precision* neutrino measurements
 - Sign of Δm^2_{23}
 - Precision determination of θ_{13}
 - Search for non-zero δ

Neutrino Factory: concept



- Intense *high-energy* neutrino source derived from muon decay
- Key accelerator systems:
 - Proton driver
 - High-power target
 - Ionisation cooling
 - Rapid acceleration

Neutrino Factory: measurements

Δm^2_{23}

$\sin^2\theta_{13}$

δ

Neutrino Factory

- $\mu^- \rightarrow \nu_\mu + \nu_e$
- $\mu^+ \rightarrow \nu_\mu + \nu_e$

■ High-energy

- Require ‘tracking’ detector
- Long ($\sim n \times 1000$ km) baseline indicated

Features:

- Beam composition known
- Energy spectrum known
- Neutrino flux measured
- 1,000 times more intense than conventional beams

$$\mu^- \rightarrow e^- \bar{\nu}_\mu \bar{\nu}_e$$

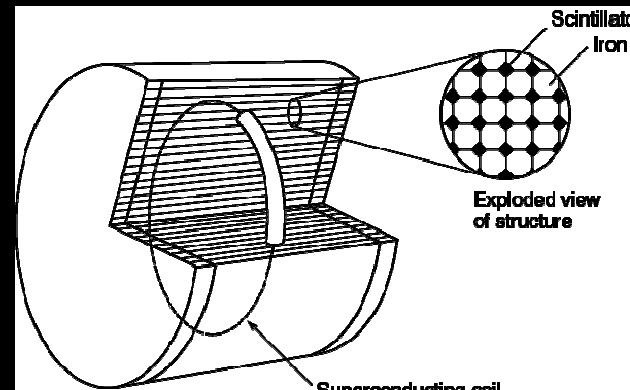
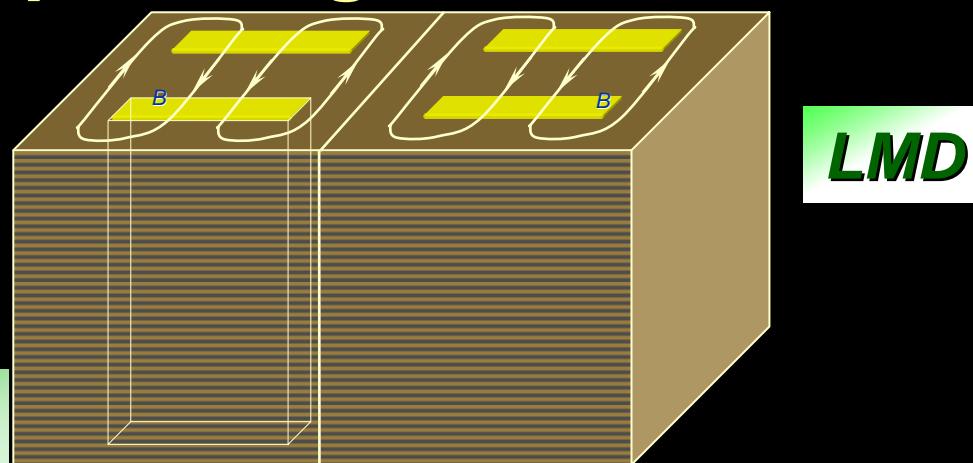
Disappearance	Appearance
$\bar{\nu}_e \rightarrow \bar{\nu}_e \rightarrow e^+$	$\bar{\nu}_e \rightarrow \bar{\nu}_\mu \rightarrow \mu^+$ $\bar{\nu}_e \rightarrow \bar{\nu}_\tau \rightarrow \tau^+$
$\nu_\mu \rightarrow \nu_\mu \rightarrow \mu^-$	$\nu_\mu \rightarrow \nu_e \rightarrow e^-$
	$\nu_\mu \rightarrow \nu_\tau \rightarrow \tau^-$

Neutrino detection:

- Assume ‘conservative’ detector:

- Fiducial mass: 50 – 100 kTon
- Event classification:
 - Charged-current electrons/positrons
 - Right-sign muons (disappearance measurements)
 - Wrong-sign muons (appearance measurements)
 - Events with no leptons (neutral current)

- Example: magnetic calorimeters

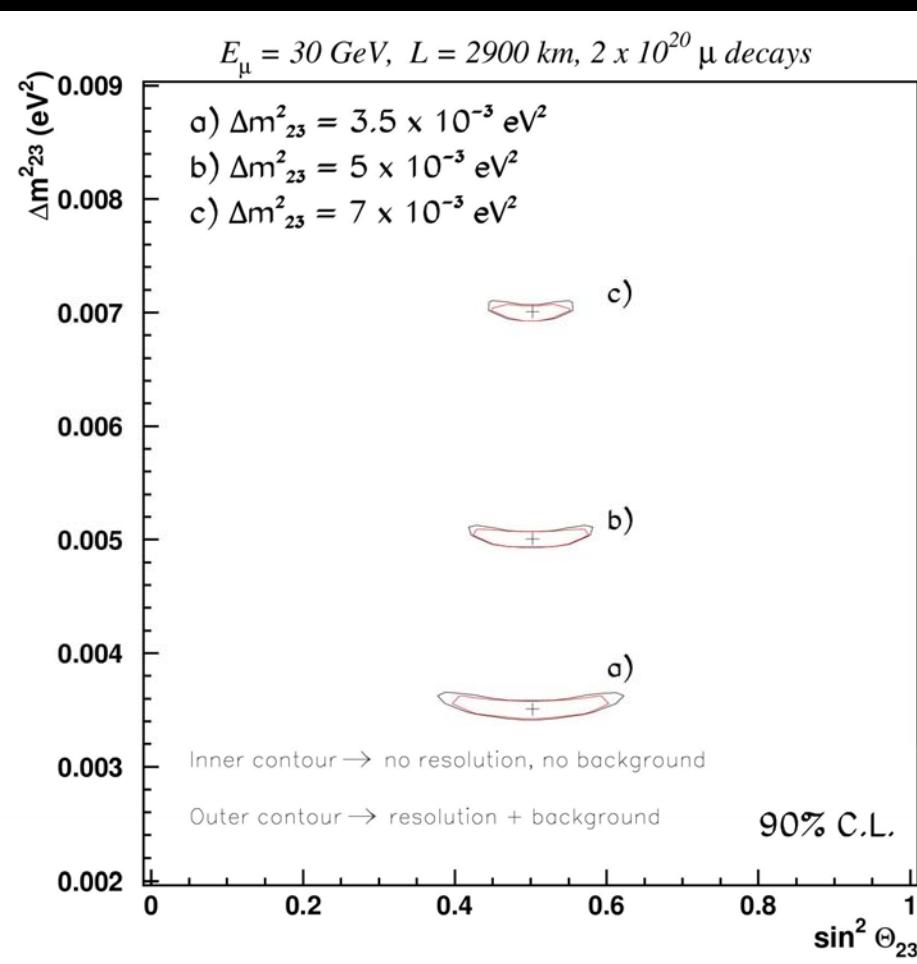
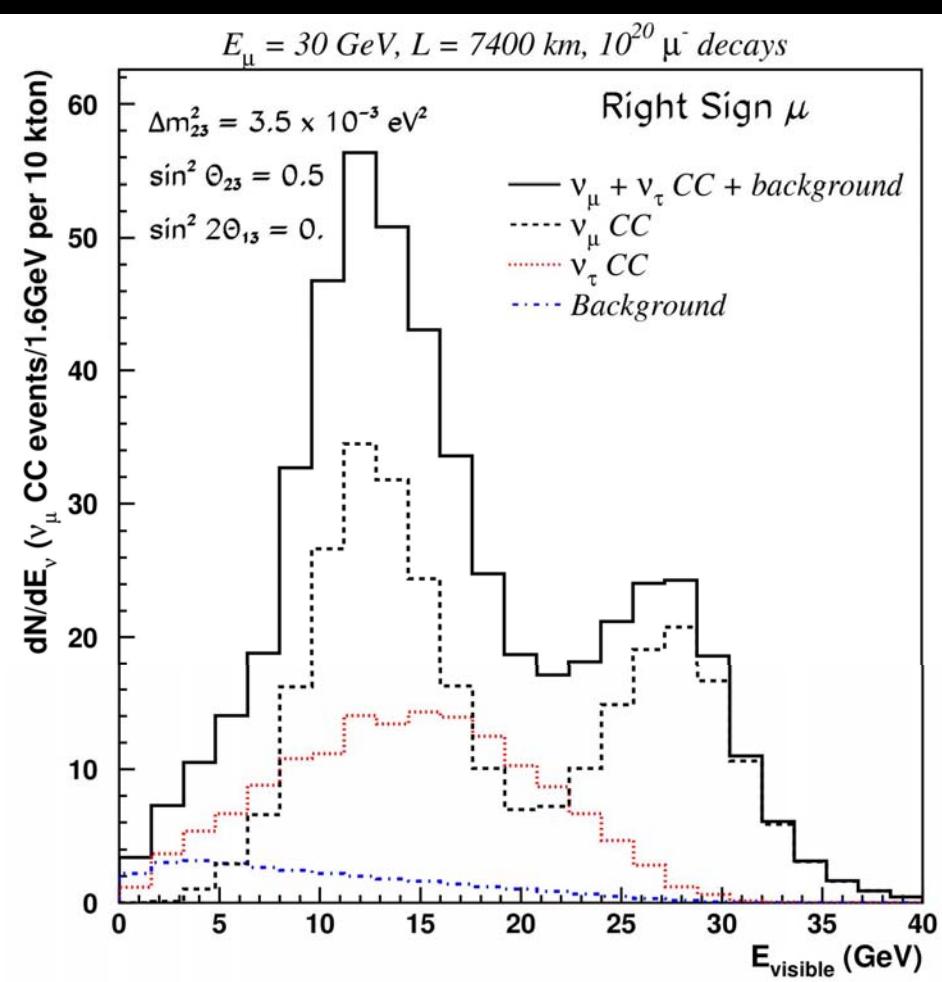


Monolith

Dimension: radius 10 m, length 20 m
Mass: 40 kt iron, 500 t scintillator

Δm^2_{23} $\sin^2 \theta_{13}$ δ

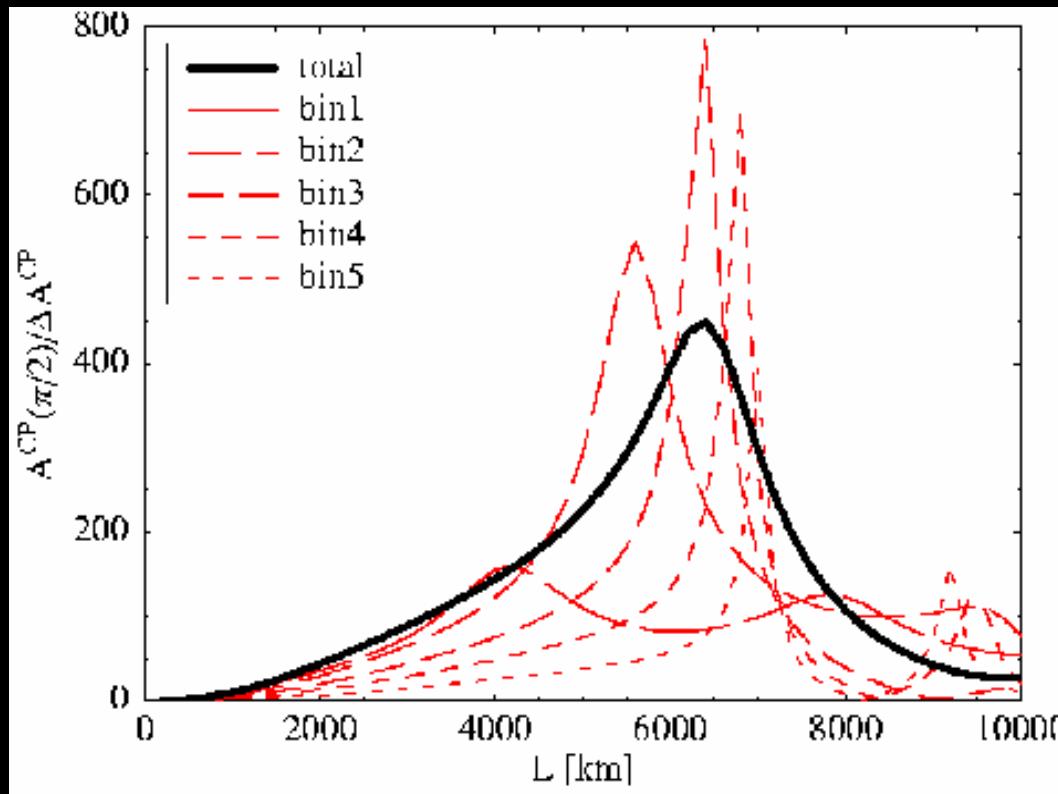
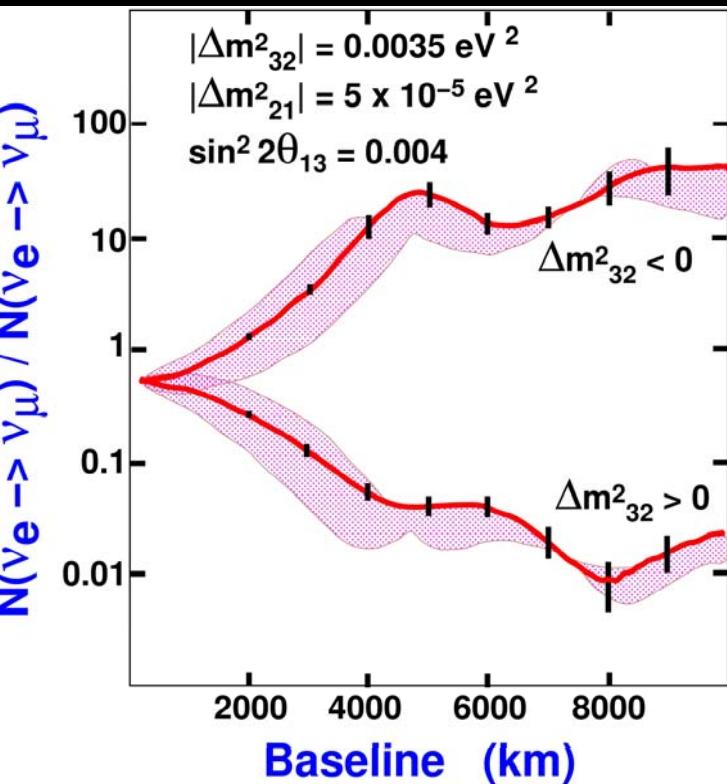
- Right-sign muons: ν_μ disappearance
- Background at or below 1 in $10^{-5} - 10^{-4}$



Δm^2_{23} $\sin^2\theta_{13}$ δ

■ Measurement of sign of Δm^2_{23}

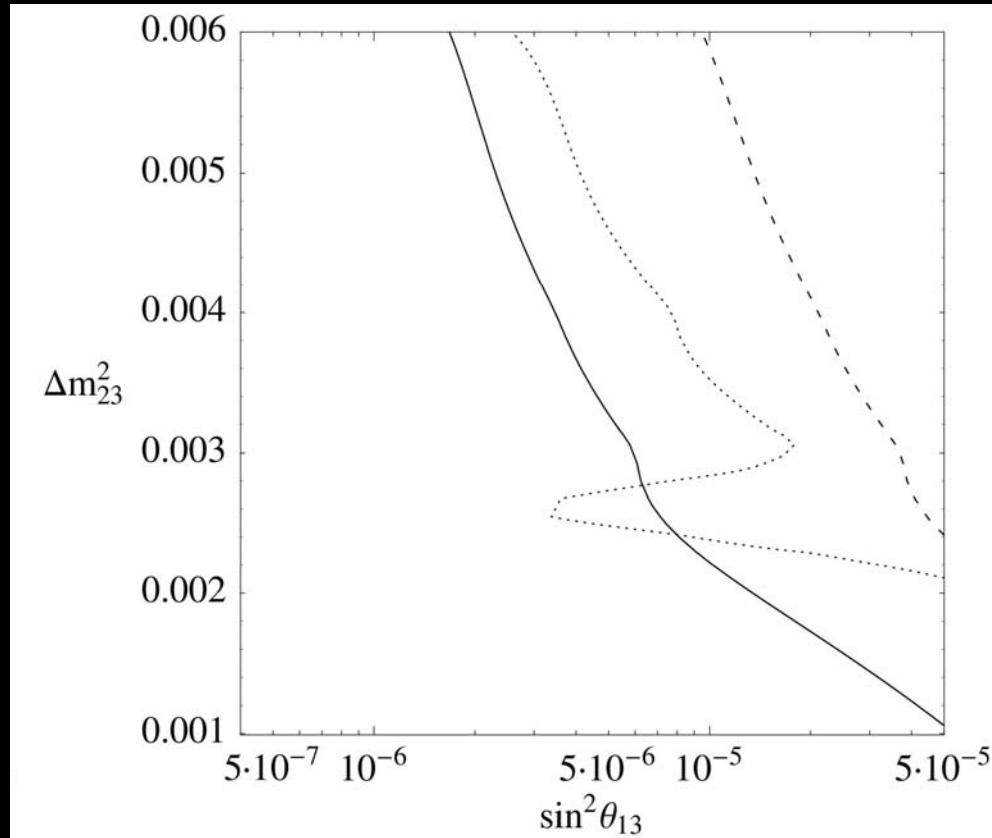
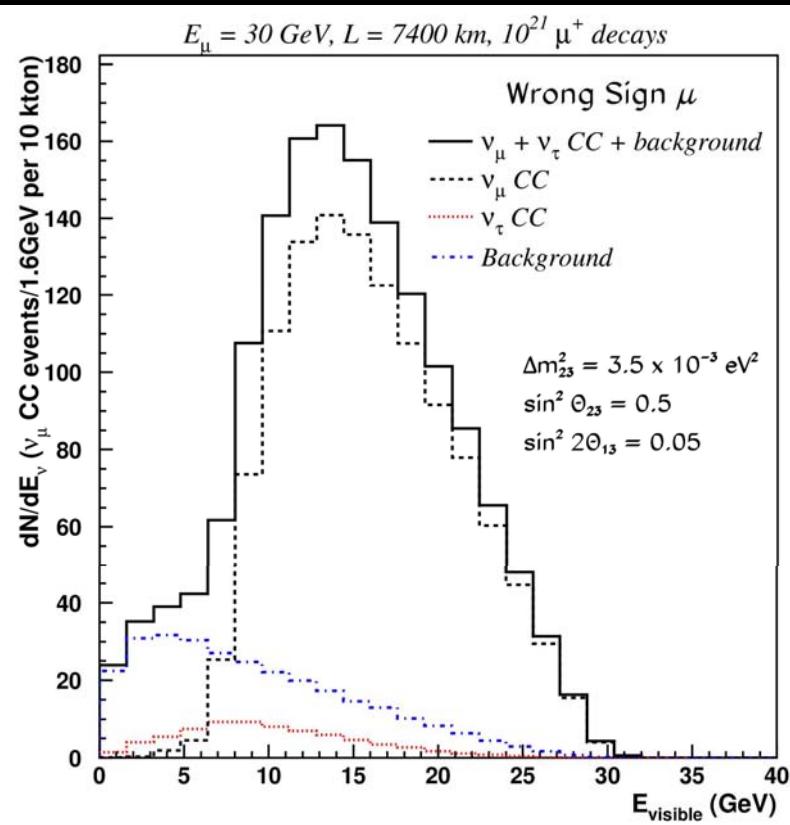
- Wrong-sign muon events: $\nu_e \rightarrow \nu_\mu$
- Electron neutrino interactions with matter different from electron-antineutrino interactions
- Requires baseline in excess of 1000 km



Δm^2_{23} $\sin^2\theta_{13}$ δ

■ θ_{13} : mixing of electron neutrinos with muon and tau neutrinos

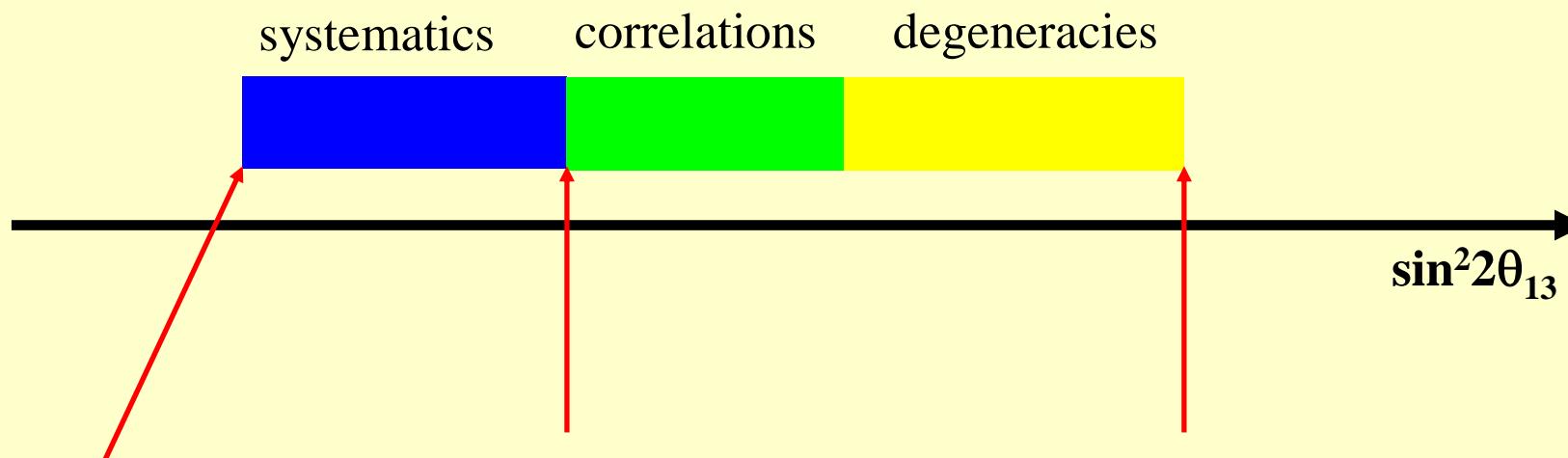
- Wrong-sign muon events: $\nu_e \rightarrow \nu_\mu$
- Background at the level of $10^{-6} - 10^{-5}$



Δm^2_{23} $\sin^2\theta_{13}$ δ

■ Determine parameters from fit:

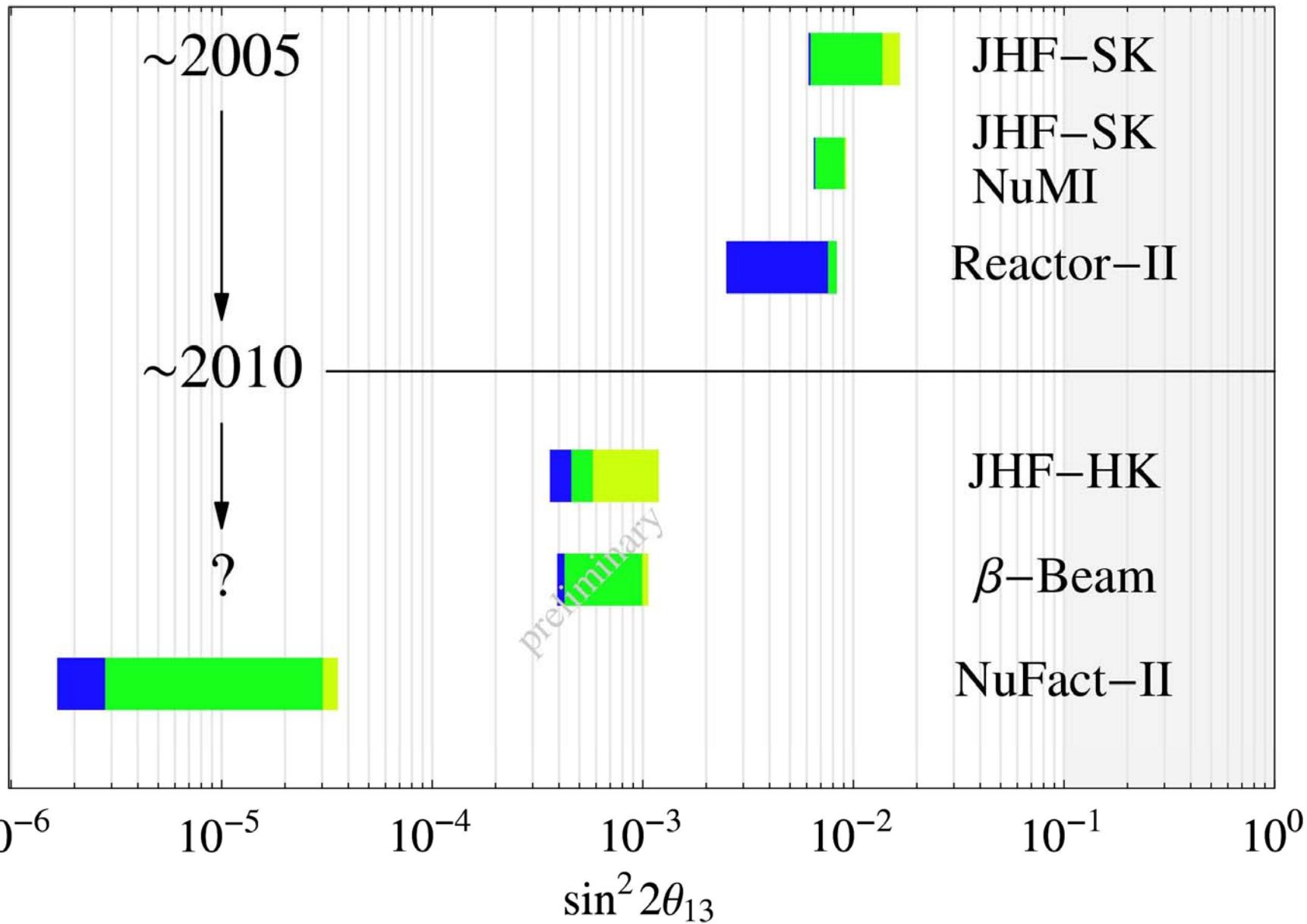
- Include more than one data set
- Several parameters are determined in fit
- Leads to:
 - Correlations among the parameters
 - Degenerate solutions (same χ^2 for >1 solutions)



**statistical limit
(all parameters fixed)**

**limit for
 $(\sin^2 2 \theta_{13})_{\text{eff}}$**

**limit for $\sin^2 2 \theta_{13}$ from
THIS experiment only**

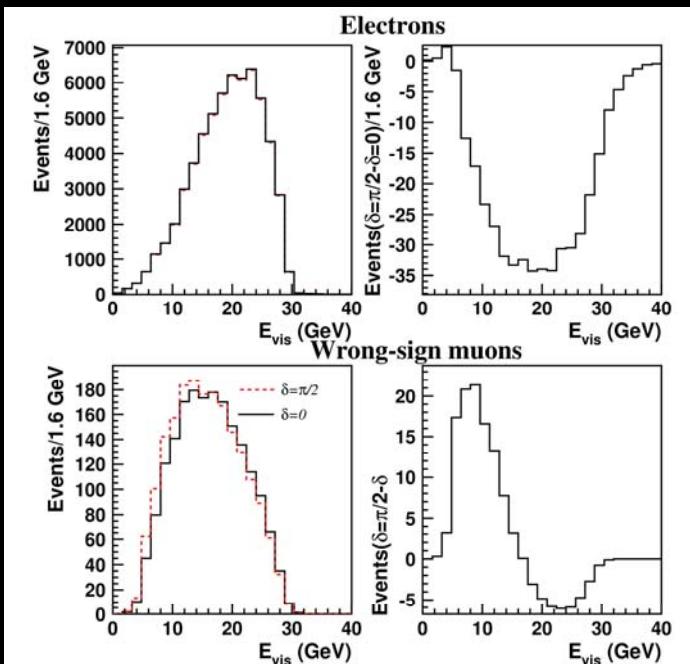
Δm^2_{23} $\sin^2\theta_{13}$ δ 

Δm^2_{23} $\sin^2\theta_{13}$ δ

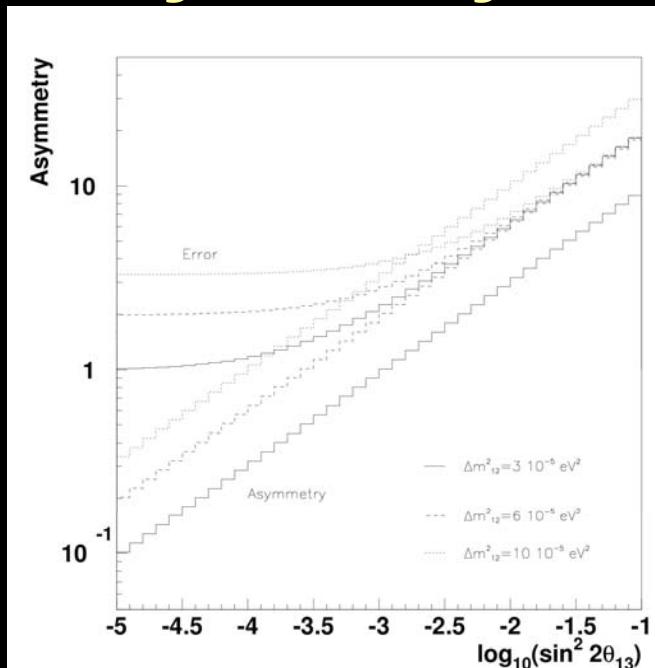
■ Measure asymmetry:

$$A^{CP} = \frac{\left\{ \frac{N(\mu^-)}{N_0(e^-)} \right\}_{\mu^-} - \left\{ \frac{N(\mu^+)}{N_0(e^+)} \right\}_{\mu^-}}{\left\{ \frac{N(\mu^-)}{N_0(e^-)} \right\}_{\mu^-} + \left\{ \frac{N(\mu^+)}{N_0(e^+)} \right\}_{\mu^-}}$$

■ Data sample:

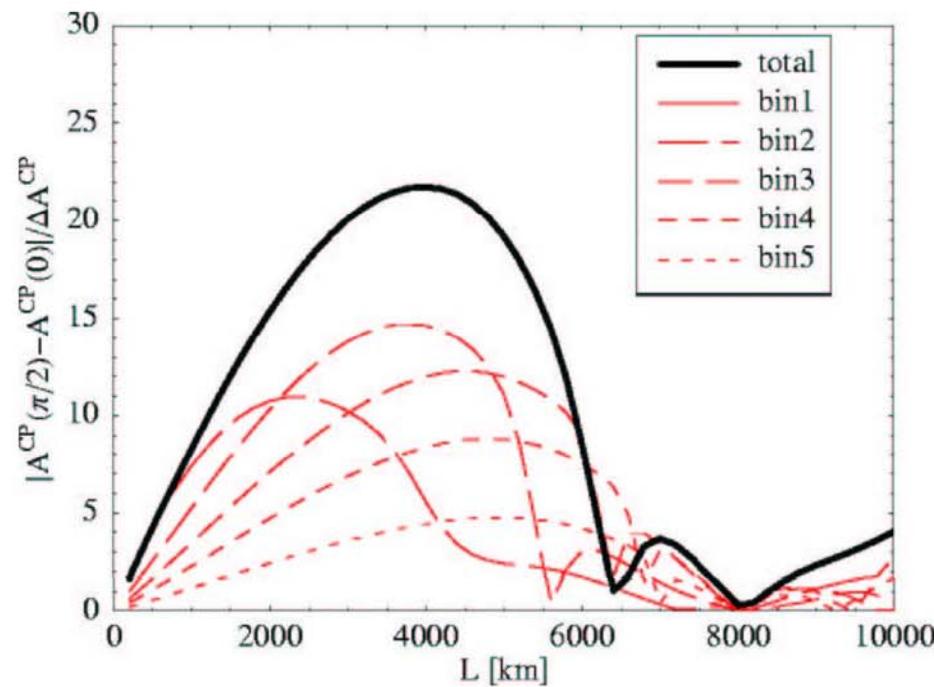
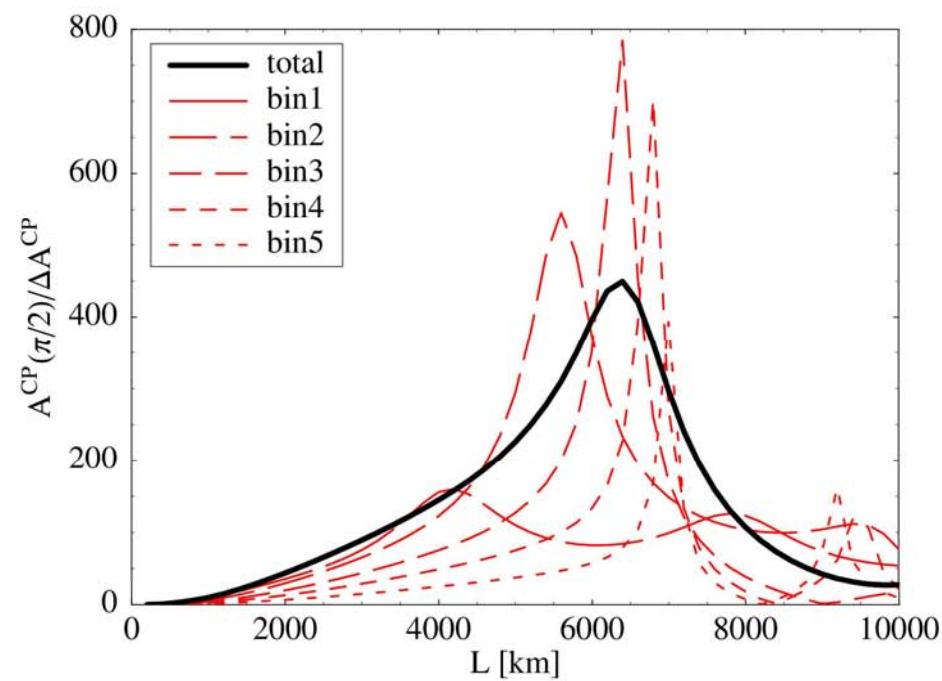


Asymmetry:

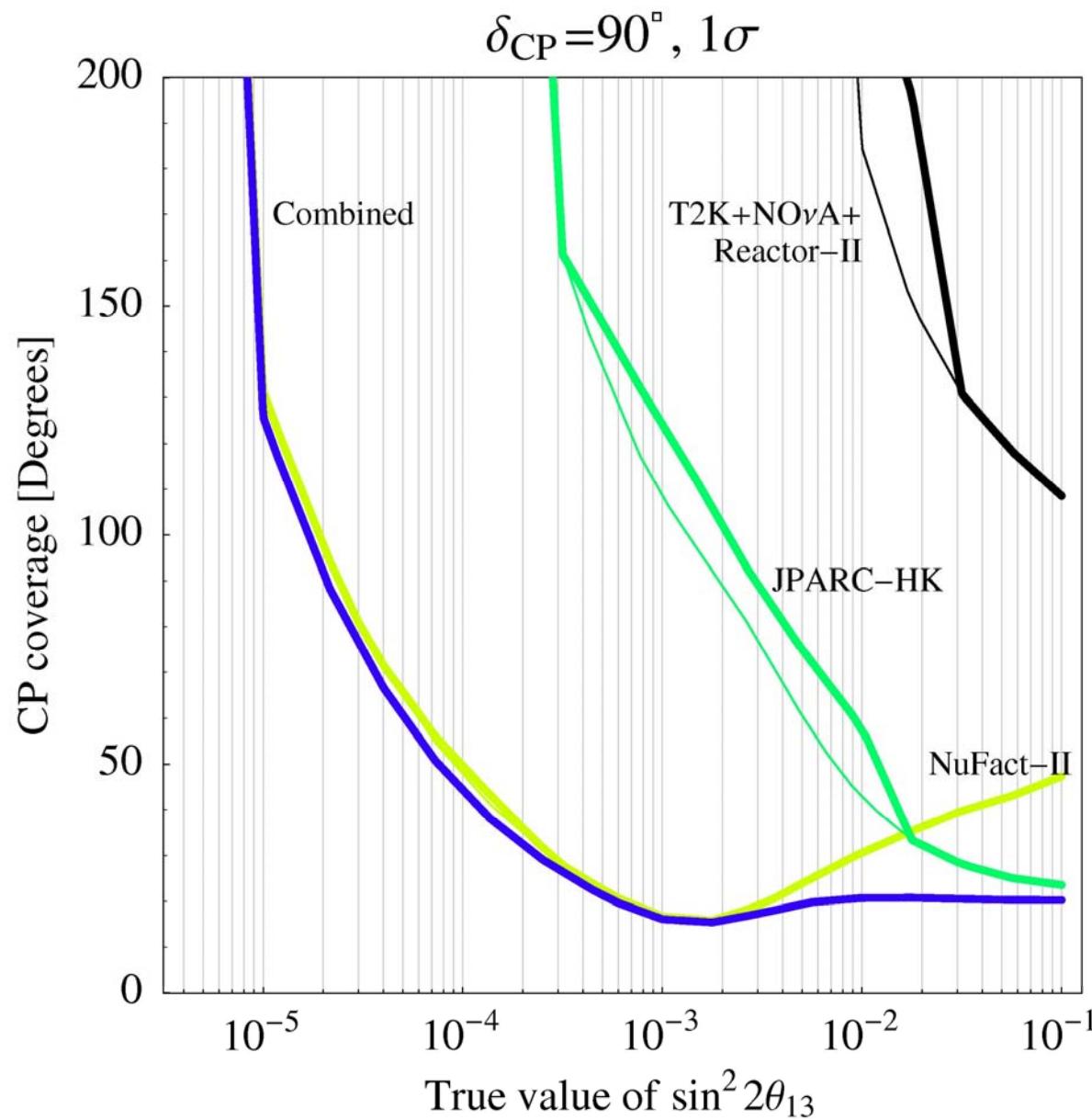


Δm^2_{23} $\sin^2 \theta_{13}$ δ

- CP asymmetry significance in the absence of ‘theoretical uncertainties’

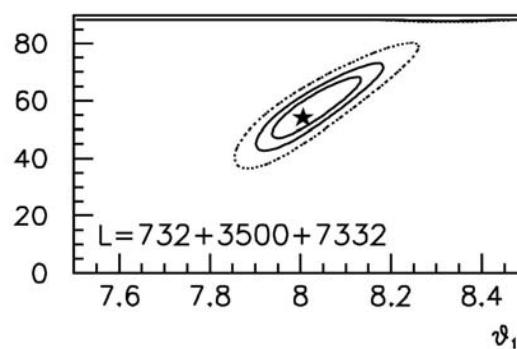
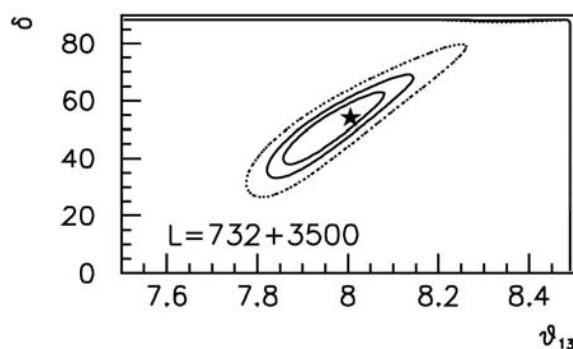
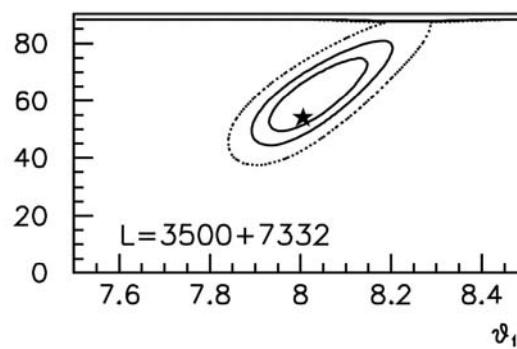
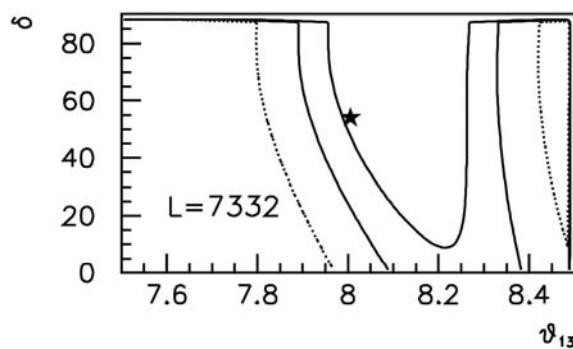
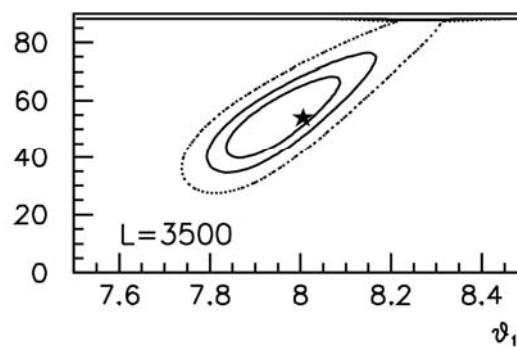
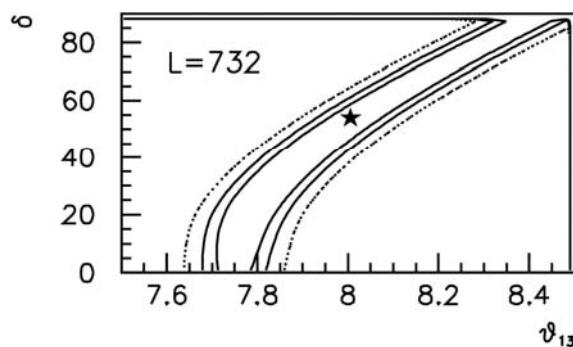


- Need to determine θ_{13} , δ simultaneously
 - Account for correlations and degeneracies

Δm^2_{23} $\sin^2\theta_{13}$ δ 

Δm^2_{23} $\sin^2\theta_{13}$ δ

■ Neutrino Factory alone; multiple baselines:



Trade off:

- Sensitivity:
 - Minimum muon energy
- Background rejection
 - Muon energy cut

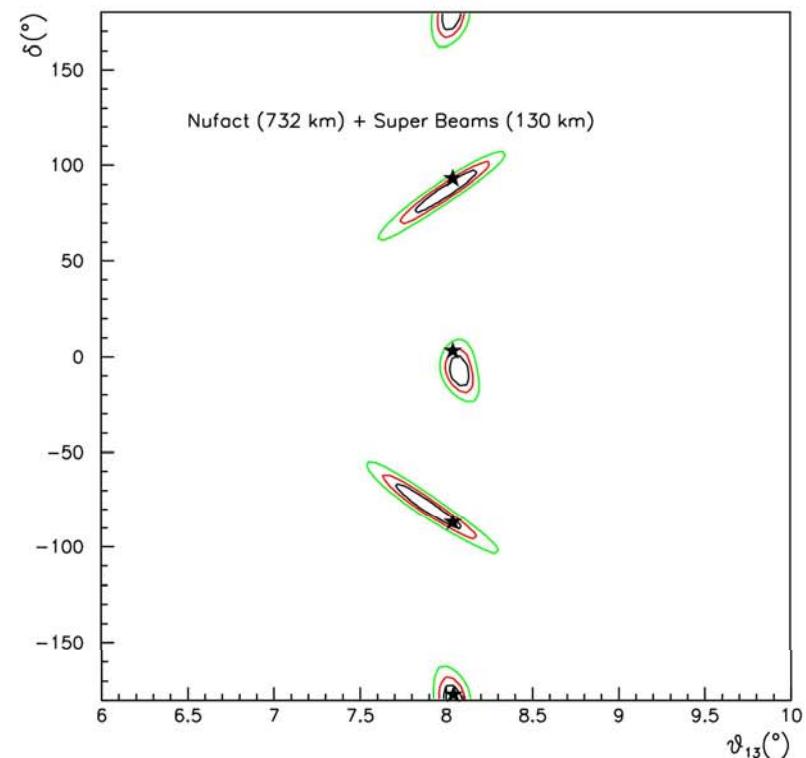
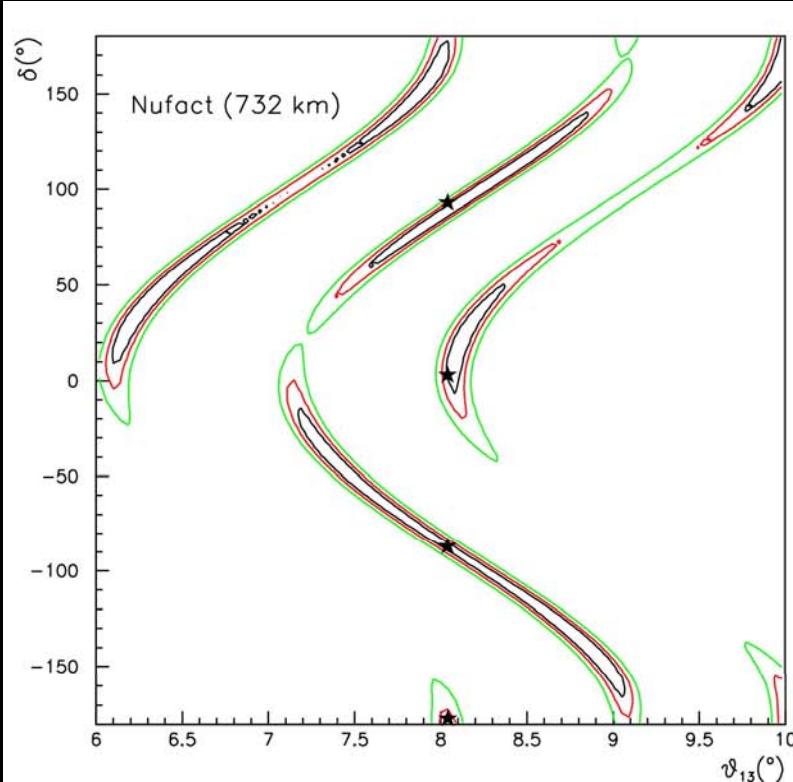
Δm^2_{23} $\sin^2\theta_{13}$ δ

Degeneracy:

Several classes:

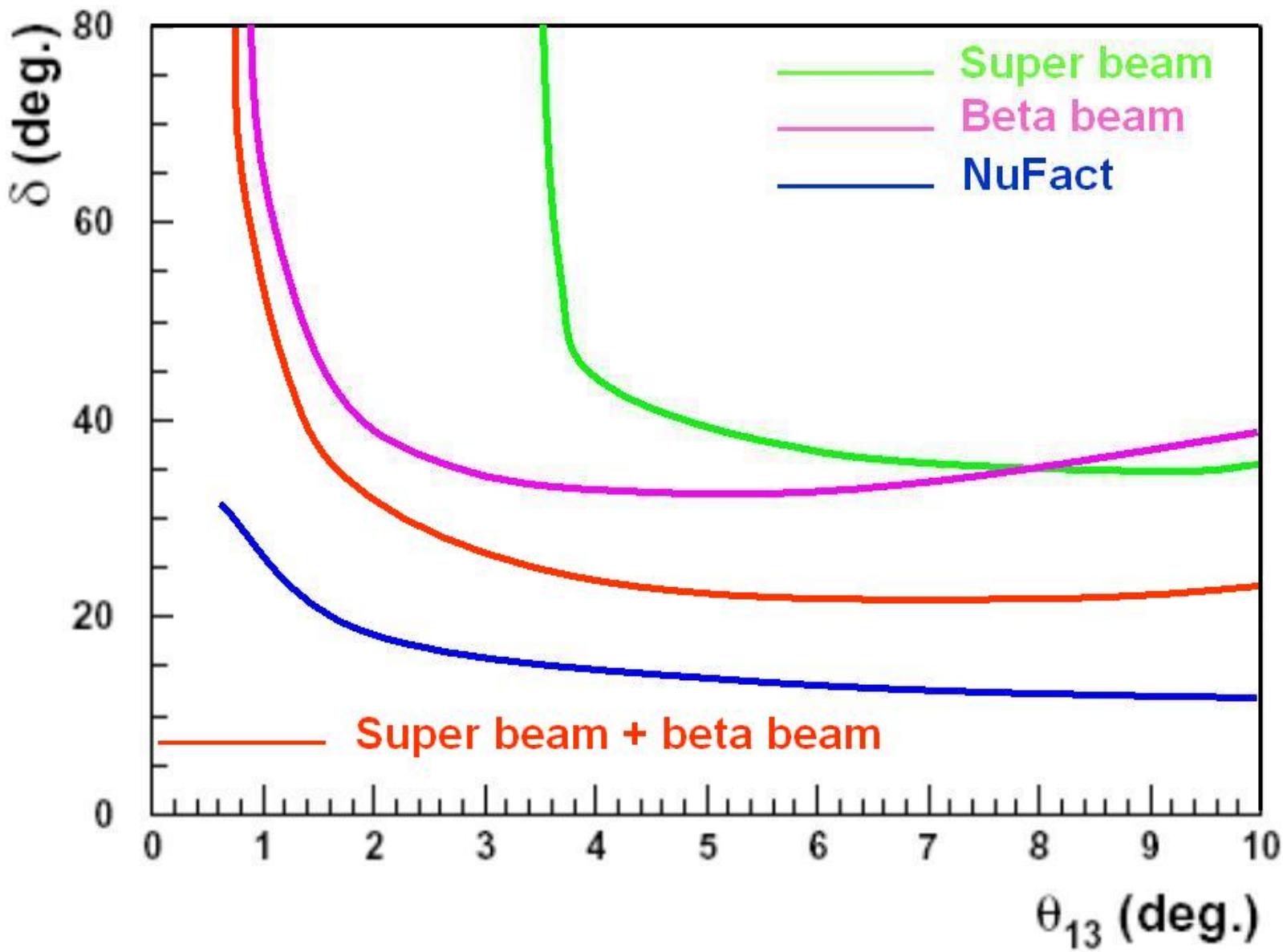
- Continuous parameters: θ_{13} , δ
- Discrete parameters: $\text{sign}(\Delta m^2_{23})$, $\text{sign}(\tan(2\theta_{23}))$

Include other channels or other experiments



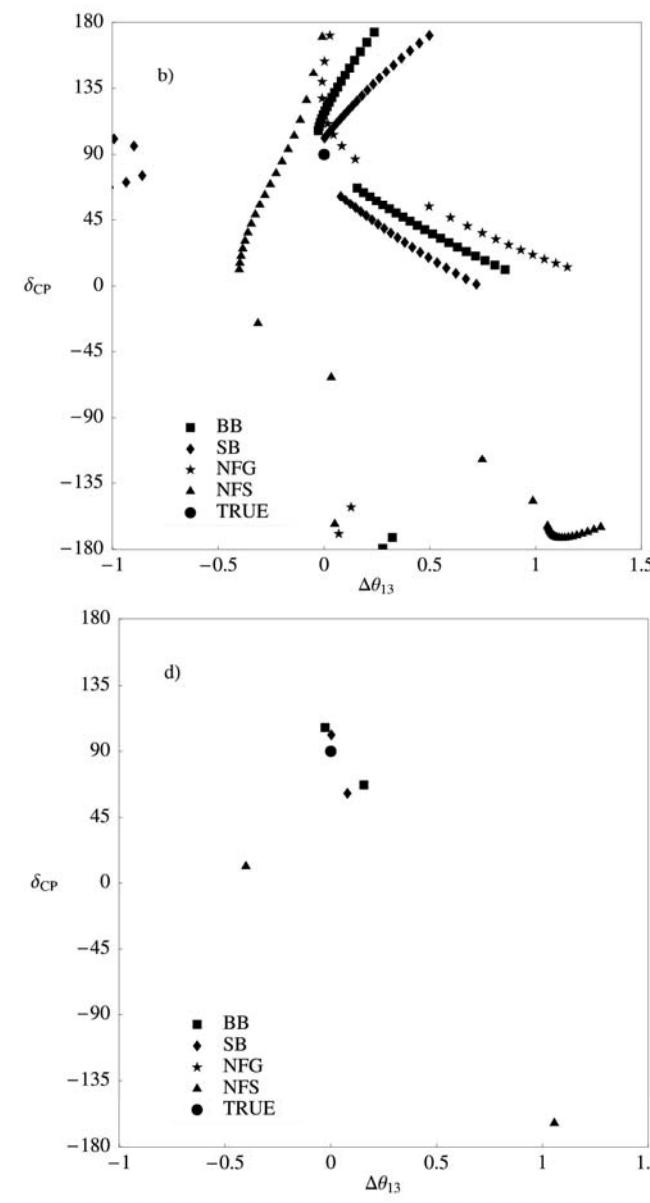
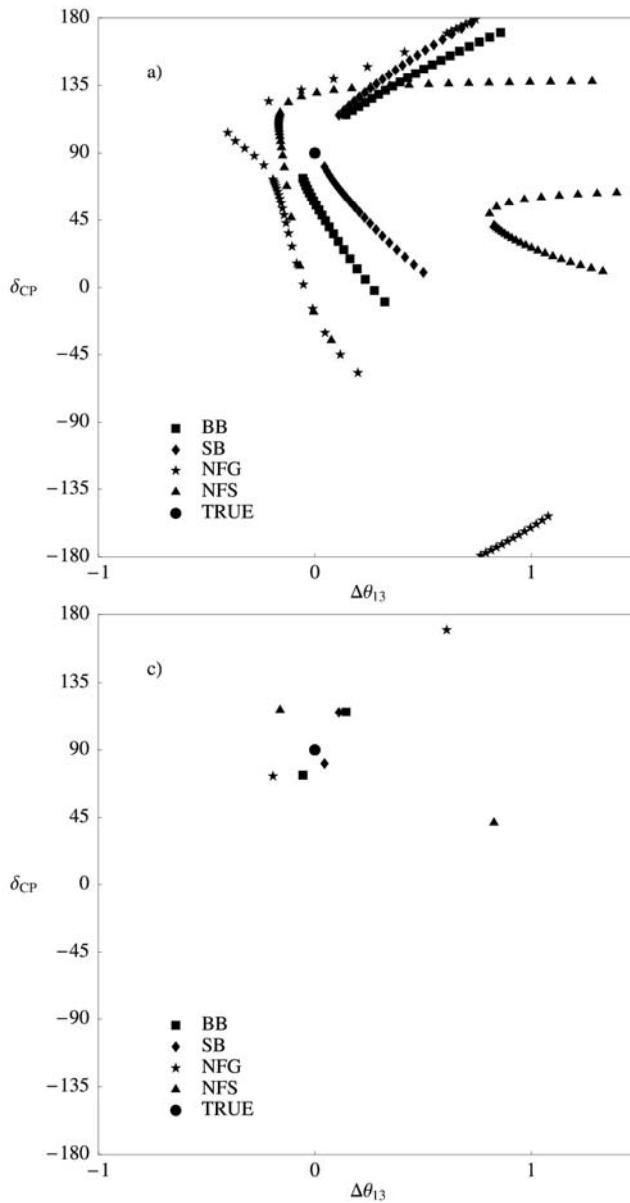
Δm^2_{23} $\sin^2\theta_{13}$ δ

3 sigma sensitivity



Δm^2_{23} $\sin^2\theta_{13}$ δ

- Other channels:
 - Golden channel: wrong sign muons
 - Silver channel: tau appearance
- Other facilities:
 - Super beam
 - Beta beam



Conclusions

- Next generation super-beam experiments:
 - First measurement of θ_{13}
- Neutrino Factory allows:
 - Precise measurements of oscillation parameters
 - Most sensitive search for leptonic CP violation
- Neutrino Factory alone:
 - Measure θ_{13} ; potential to discover $\delta \neq 0$
 - Can not resolve all degeneracies
 - Requires super beam or beta beam
- Need for design studies:
 - Need to understand sensitivities and limitations of each facility on equal footing
 - Need to compare performance and cost
 - Need for robust design studies of:
 - Beta beam
 - Neutrino Factory

So allow a consensus plan for an exciting future to emerge