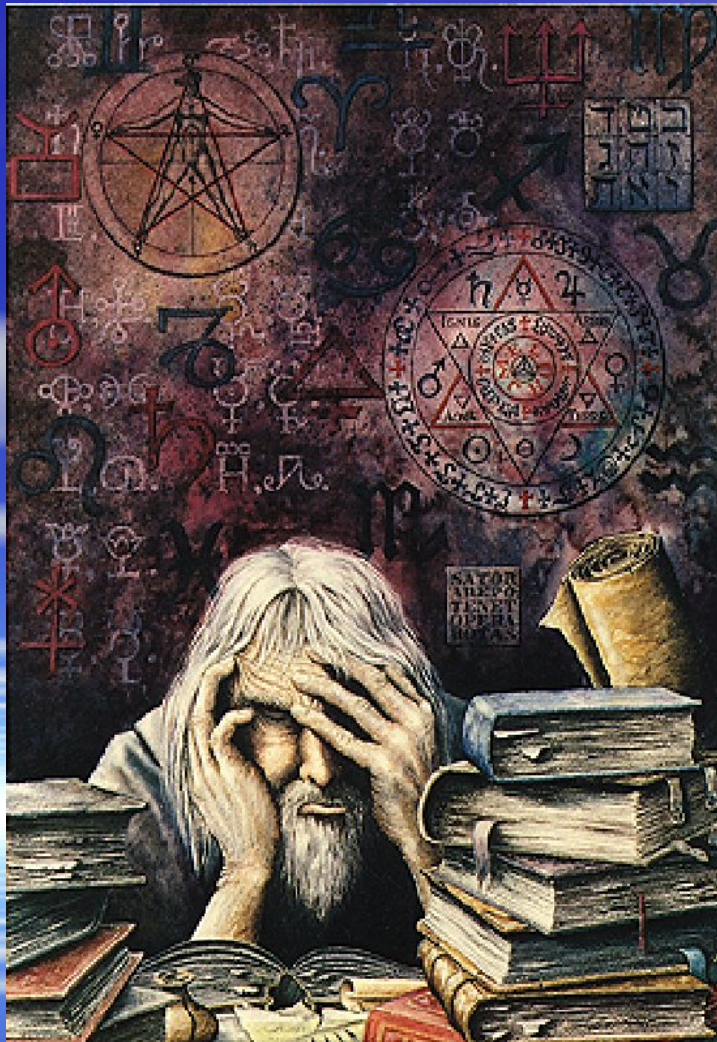


Absolute Neutrino Mass Measurements

Kai Zuber
Univ. of Oxford/ Univ. of Sussex

Contents



- Beta decay
- Double beta decay
- Cosmological neutrino mass bounds
- Summary and conclusions

Oscillation evidences

LSND

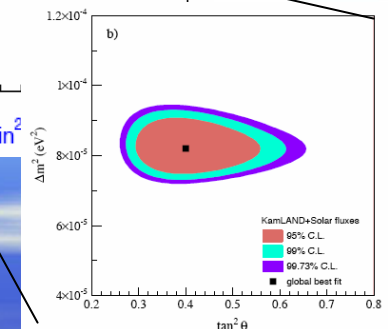
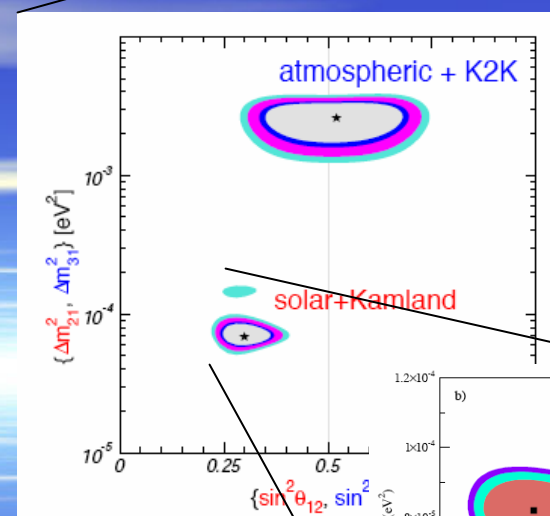
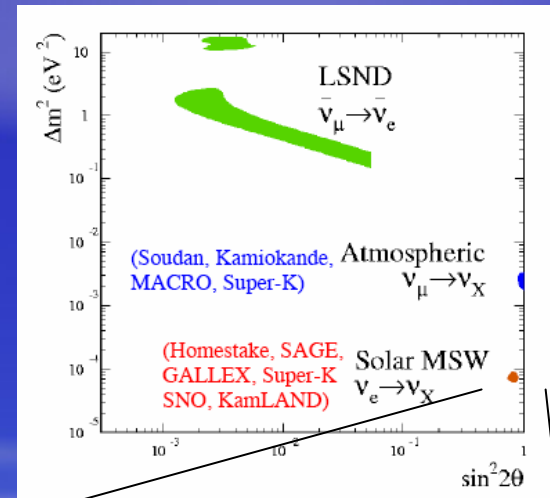
$$\sin^2 2\theta = 10^{-1}-10^{-3}, \Delta m^2 = 0.1-6 \text{ eV}^2$$

Atmospheric

$$\sin^2 2\theta = 1.00, \Delta m^2 = 2.1 \times 10^{-3} \text{ eV}^2$$

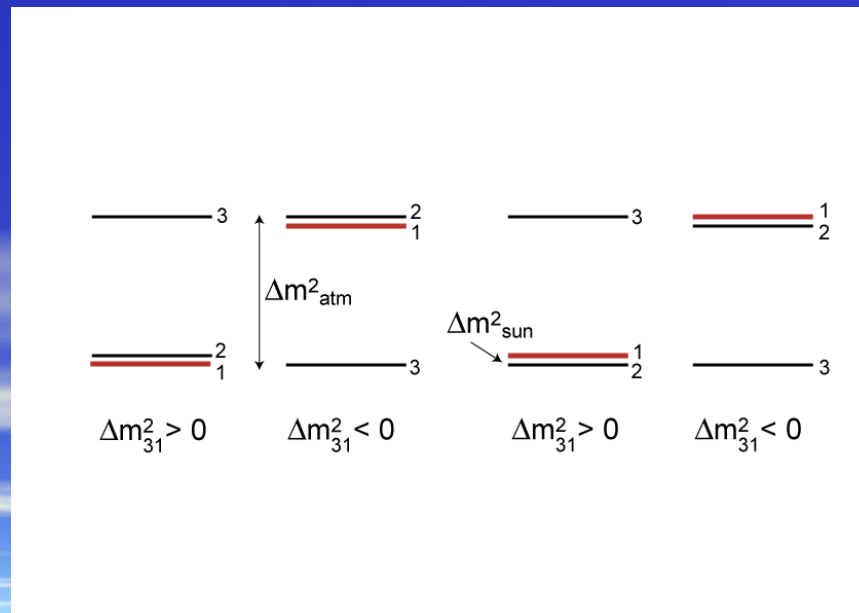
Solar + reactors

$$\sin^2 2\theta = 0.81, \Delta m^2 = 8.2 \times 10^{-5} \text{ eV}^2$$



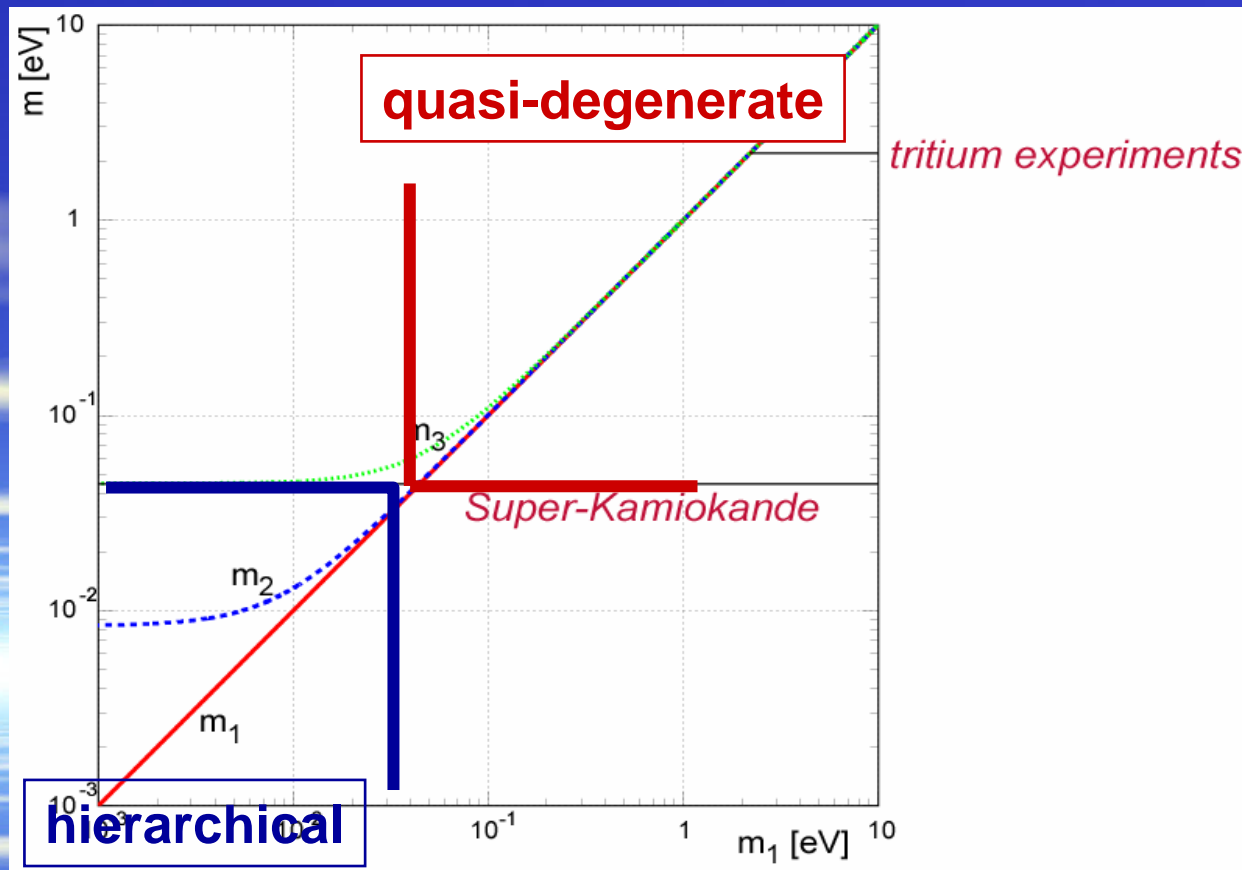
If all three are correct... we need more (sterile ones)

Models of neutrino masses



Neutrino mass schemes

„normal“ mass hierarchy $m_1 < m_2 < m_3$



Current neutrino mass limits

Direct kinematical limits

^3H decay: $m_{\nu e} < 2.3 \text{ eV}$

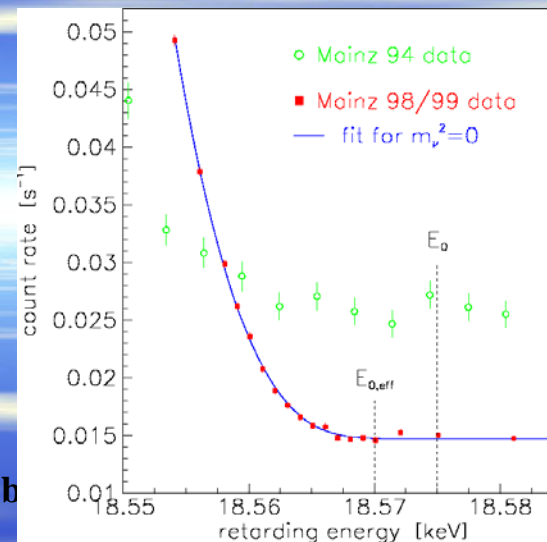
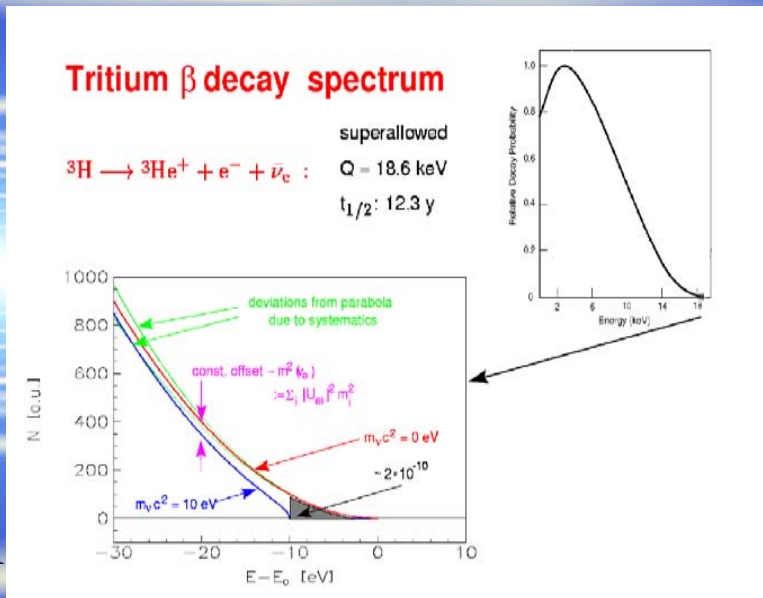
Mainz, Troitzk

Pion decay: $m_{\nu\mu} < 190 \text{ keV}$

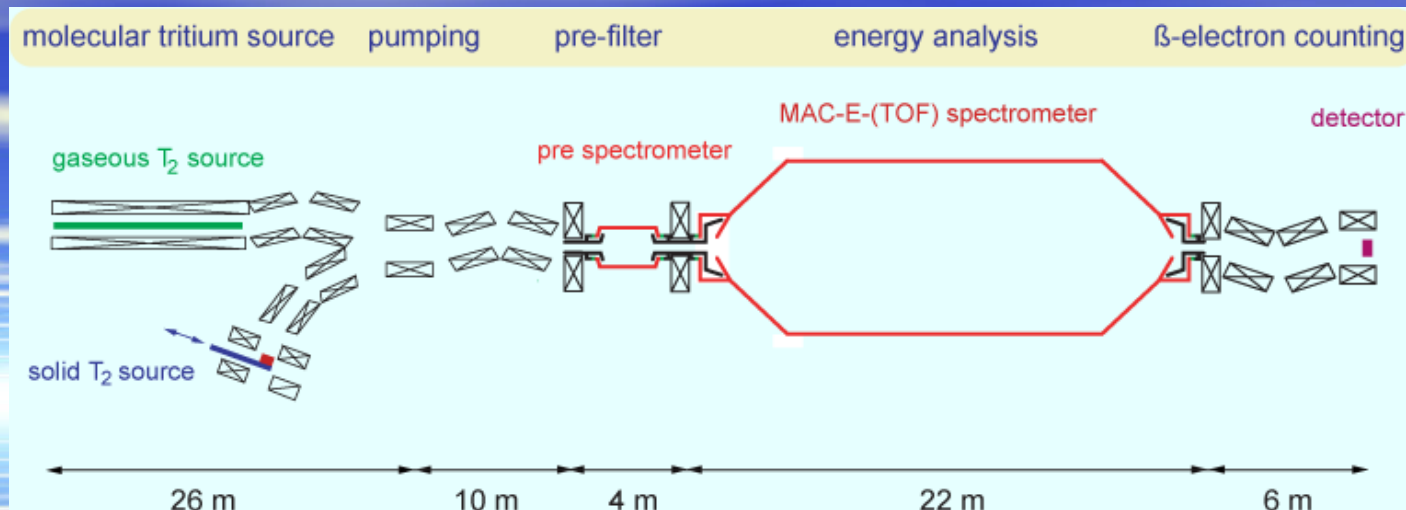
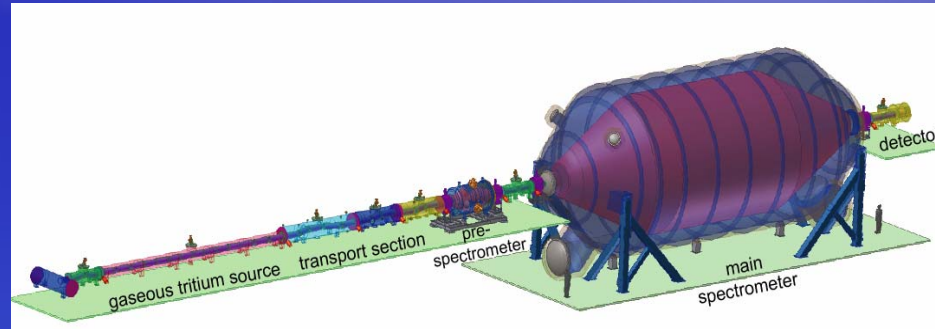
PSI

Tau decay: $m_{\nu\tau} < 18.2 \text{ MeV}$

LEP (Aleph)



KATRIN-The ultimate beta-decay experiment



Discovery potential $m_{\nu e} = 0.35 \text{ eV}$ at 5σ

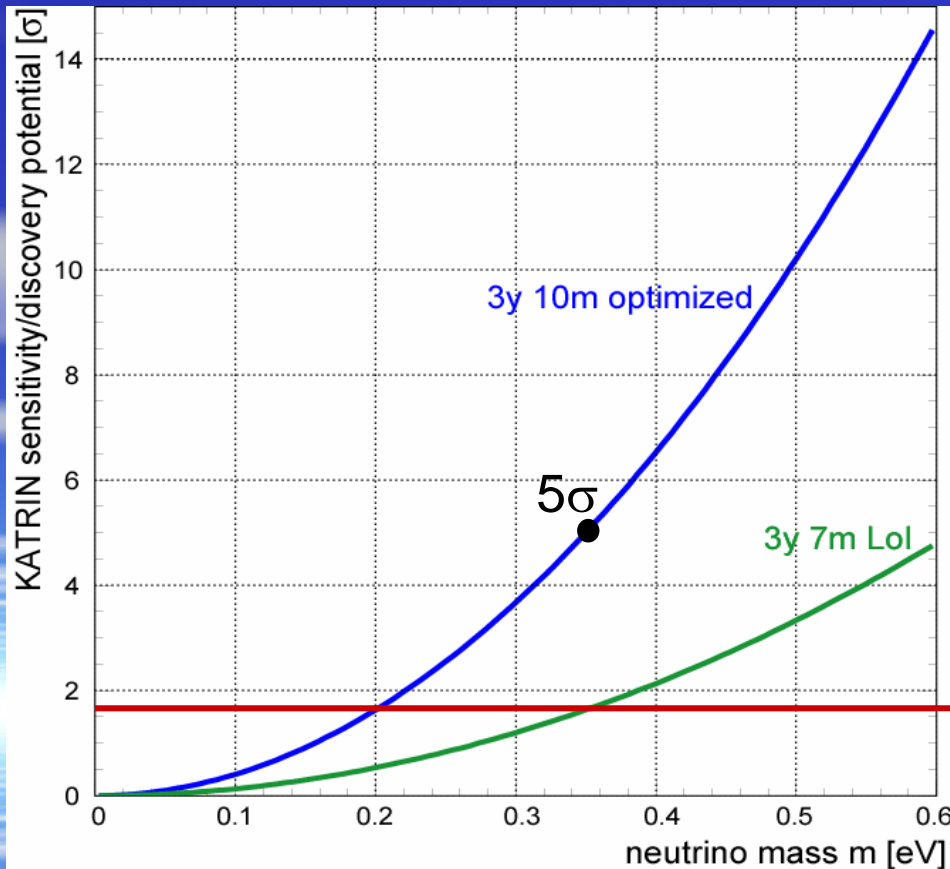
Sensitivity $m_{\nu e} < 0.2 \text{ eV}$ (90% CL)

Commissioning in 2008

18. Jan. 2005

Workshop on beta beams, RAL

KATRIN sensitivity & discovery potential



expectation:

after 3 full beam years

$$\sigma_{\text{syst}} \sim \sigma_{\text{stat}}$$

$$m_{\nu} = 0.35\text{eV} (5\sigma)$$

$$m_{\nu} = 0.3\text{eV} (3\sigma)$$

discovery potential

$$m_{\nu} < 0.2\text{eV} (90\%\text{CL})$$

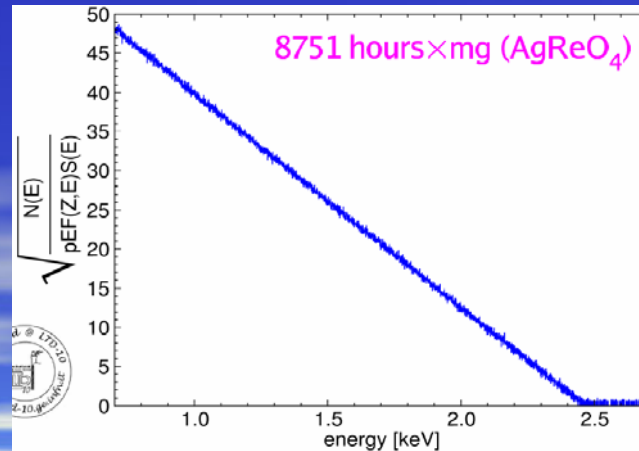
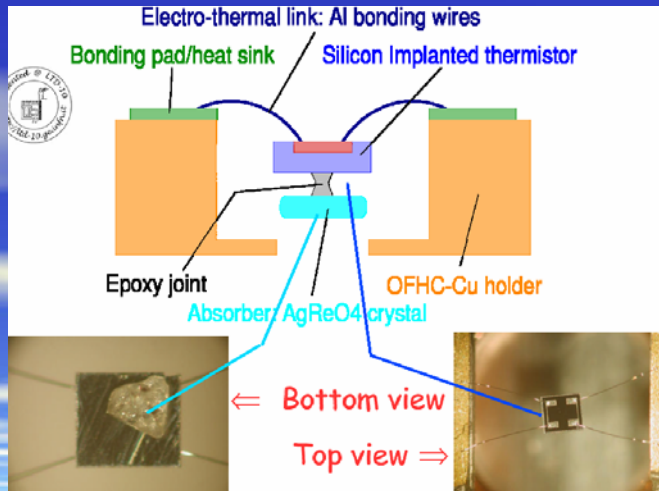
sensitivity

Alternative approaches I



$$n(Q - \Delta E) \propto \left(\frac{\Delta E}{Q} \right)^3$$

μ -calorimeters working at mK



MIBETA,
Genova

$$Q = 2465.3 \pm 0.5_{\text{stat}} \pm 1.6_{\text{syst}} \text{ eV}$$

(8751 h*mg, NIMA520, 2004)

$$= 2466.1 \pm 0.8_{\text{stat}} \pm 1.5_{\text{syst}} \text{ eV}$$

(4485 h*mg, PRL91,2003)

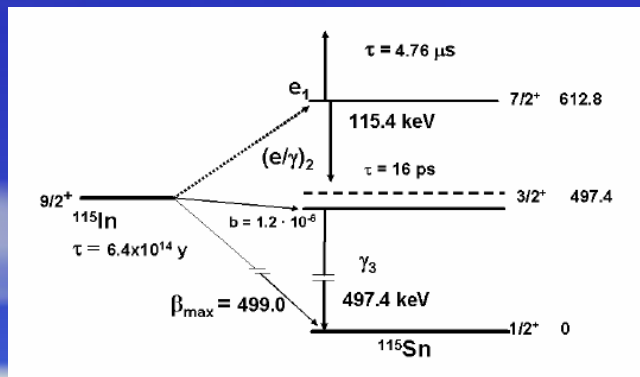
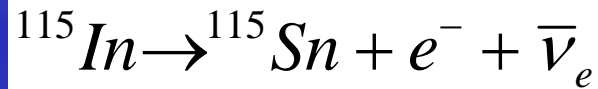
$$m_\nu^2 = -112 \pm 207 \pm 90 \text{ eV}^2$$

$$m_\nu < 15 \text{ eV (90\%CL)}$$

future:

proposal for a new calorimeter expt. with
~2-3 eV sensitivity
foreseen 2007 (?)

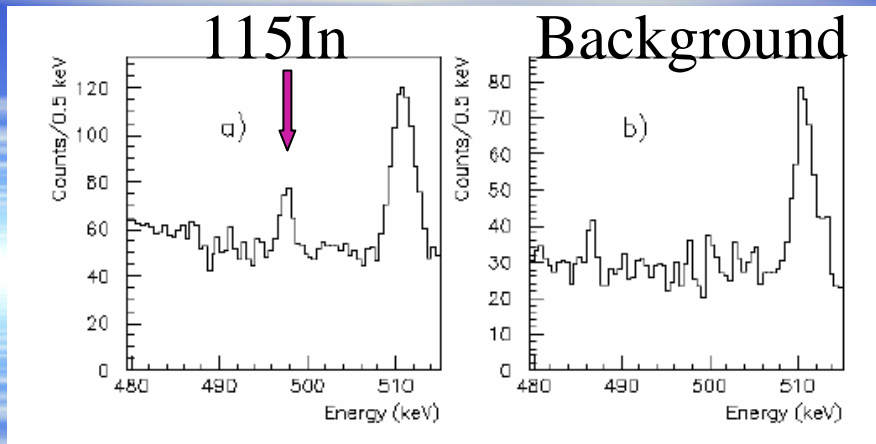
Alternative approaches II



Observed line at 497.4 keV within test measurements for LENS

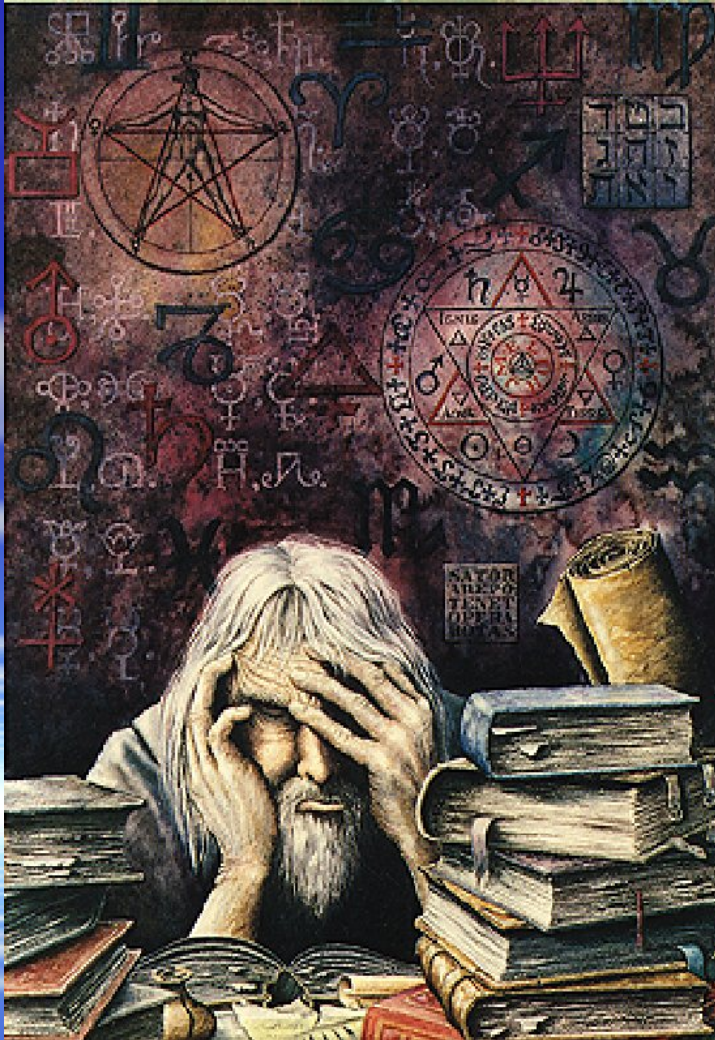
If real a Q-value for beta decay of 2 ± 4 keV

Origin of line has to be verified



C. M. Cattadori et al, nucl-ex/0407016

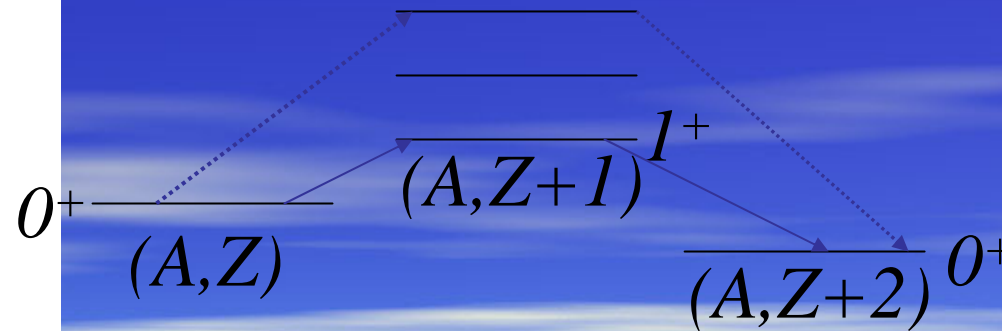
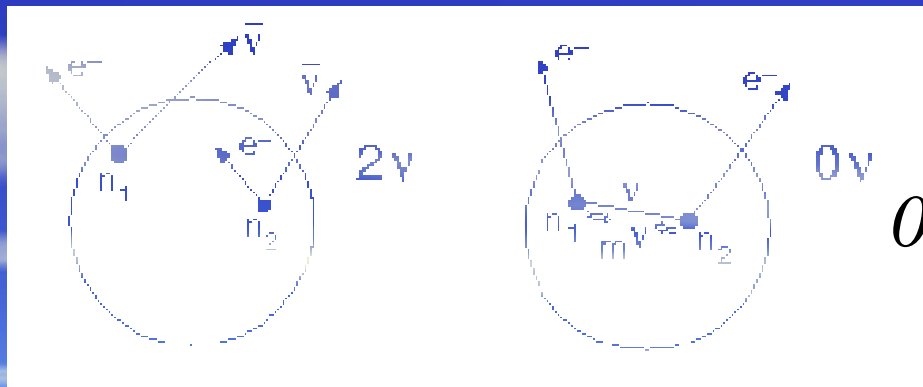
Contents



- Beta decay
- Double beta decay
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Double beta decay

- $(A, Z) \rightarrow (A, Z+2) + 2 e^- + 2 \bar{\nu}_e$ $2\nu\beta\beta$
- $(A, Z) \rightarrow (A, Z+2) + 2 e^-$ $0\nu\beta\beta$



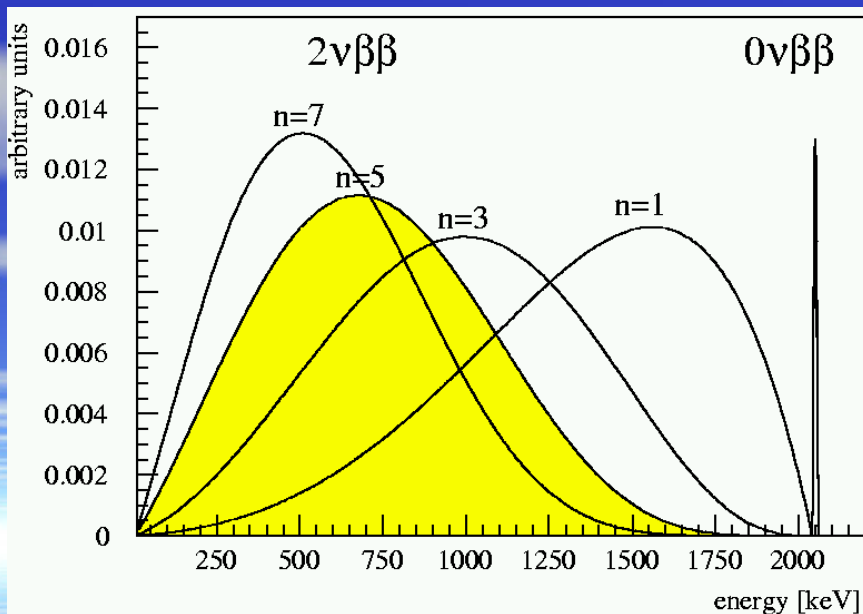
In nature there are 35 isotopes

$2\nu\beta\beta$: Seen in 10 isotopes, important for nuclear physics input

$0\nu\beta\beta$: Only possible if neutrinos are Majorana particles

Spectral shapes

$0\nu\beta\beta$: Peak at Q-value of nuclear transition



Measured quantity: Half-life

Dependencies (BG limited)

$$T_{1/2} \propto a \cdot \varepsilon (M \cdot t / \Delta E \cdot B)^{1/2}$$

link to neutrino mass

$$1 / T_{1/2} = PS * NME^2 * (m_\nu / m_e)^2$$

Sum energy spectrum of both electrons

3 Flavour oscillations (PMNS)

Analogous to CKM matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \Rightarrow \frac{m_i^2}{2E_\nu} \Rightarrow \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

$$U = \begin{pmatrix} \cos\theta_{12} & \sin\theta_{12} & 0 \\ -\sin\theta_{12} & \cos\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \cos\theta_{13} & 0 & \sin\theta_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -\sin\theta_{13}e^{i\delta} & 0 & \cos\theta_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{23} & \sin\theta_{23} \\ 0 & -\sin\theta_{23} & \cos\theta_{23} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\beta_1} & 0 \\ 0 & 0 & e^{i\beta_2} \end{pmatrix}$$

solar If $\sin\theta_{13} \neq 0 \rightarrow$ CP-violation atmospheric

Majorana: $U = U_{PMNS} \text{diag}(1, e^{i\alpha}, e^{i\beta})$

Physical quantities

Experimental observable: Half-life

Double beta decay: Effective Majorana neutrino mass

$$\langle m_\nu \rangle \equiv m_{ee} = \left| \sum_k U_{ek}^2 m_k \right| = \left| \sum_k |U_{ek}|^2 e^{i\alpha_{ek}} m_k \right|$$

relative CP phases = ± 1

Beta decay

$$m_e = \sum |U_{ek}|^2 m_k$$

Phase space

$0\nu\beta\beta$ decay rate scales with Q^5

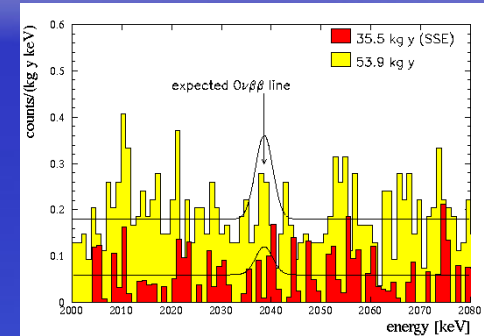
$2\nu\beta\beta$ decay rate scales with Q^{11}

<i>Isotope</i>	<i>Q-value (keV)</i>	<i>Nat. abund. (%)</i>	<i>(PS 0ν)⁻¹ (yrs)</i>	<i>(PS 2ν)⁻¹ (yrs)</i>
Ca 48	4271	0.187	4.10E24	2.52E16
Ge 76	2039	7.8	4.09E25	7.66E18
Se 82	2995	9.2	9.27E24	2.30E17
Zr 96	3350	2.8	4.46E24	5.19E16
Mo 100	3034	9.6	5.70E24	1.06E17
Pd 110	2013	11.8	1.86E25	2.51E18
Cd 116	2809	7.5	5.28E24	1.25E17
Sn 124	2288	5.64	9.48E24	5.93E17
Te 130	2529	34.5	5.89E24	2.08E17
Xe 136	2479	8.9	5.52E24	2.07E17
Nd 150	3367	5.6	1.25E24	8.41E15

Heidelberg -Moscow

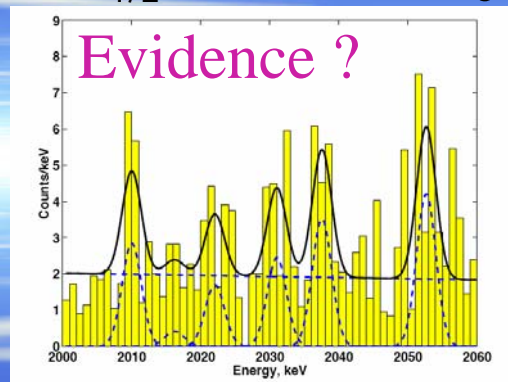


- **Five Ge Diodes (mass 10.9 kg)**
Isotopical enriched (86%) in ^{76}Ge
lead shield and nitrogen purging
Peak at 2039 keV



H.V. Klapdor-Kleingrothaus et al,
 Europ. Phys. J. A 12, 147 (2001)

$T_{1/2} > 1.9 \times 10^{25}$ yr (90% CL) \longrightarrow $m < 0.35$ eV



Subgroup of collaboration

$T_{1/2} = 0.6 - 8.4 \times 10^{25}$ yr
 \longrightarrow $m = 0.17 - 0.63$ eV

H.V. Klapdor-Kleingrothaus et al,
 Phys. Lett. B 586, 198 (2004)

If peak is real...

1.) Go out and check (GERDA, MAJORANA)

Is peak something specific to Ge?

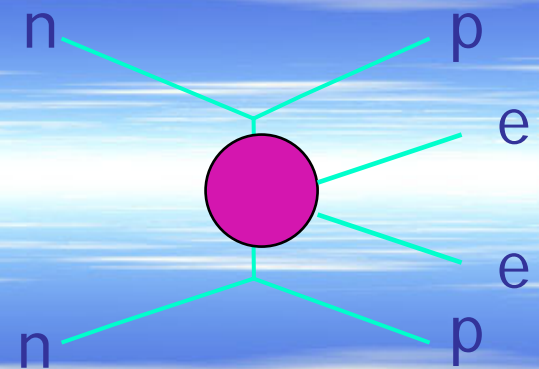
Uncertainties in the nuclear matrix elements?

→ Check with a different isotope

Physics mechanism at work ?

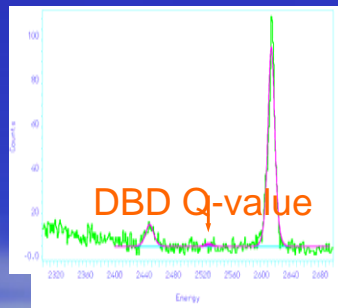
→ Tracking

2.) NEMO, COBRA



Running experiments

CUORICINO: cryogenic bolometers
40.7 kg TeO_2



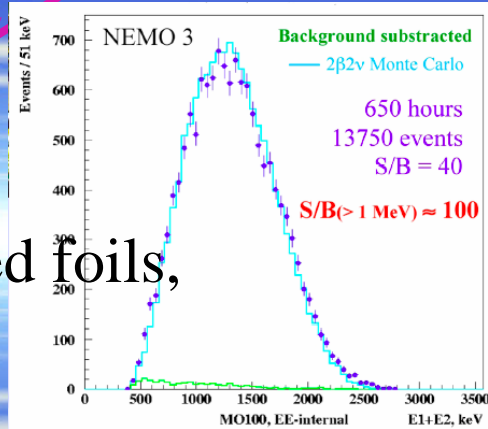
$T_{1/2} > 7.5 \times 10^{23}$ yr (90% CL)

E. Fiorini, Neutrino 2004

NEMO-3: TPC

Future: CUORE
760 kg TeO_2
approved

10 kg enriched foils,
6 kg ^{100}Mo



Idea:
Super-NEMO (100 kg)

$T_{1/2} > 3.1 \times 10^{23}$ yr (90% CL)

18. Jan. 2005

Workshop on beta beams, RAL

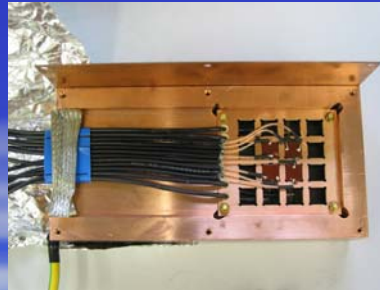
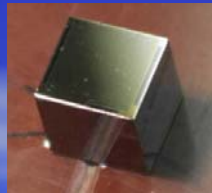
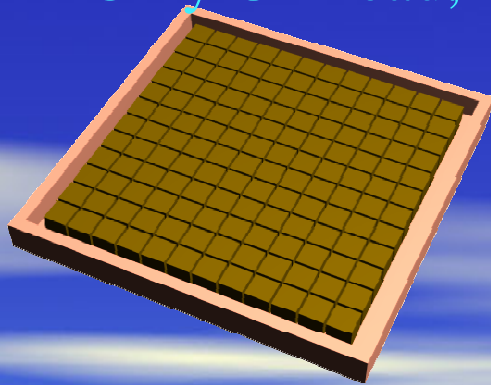
COBRA



Use CdZnTe semiconductors

Only UK lead, UK dominated experiment

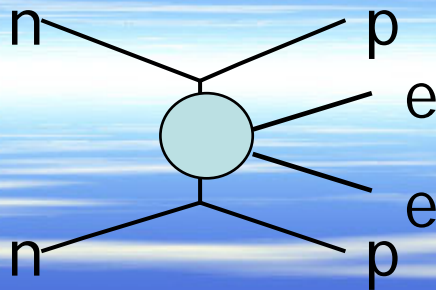
already 5 world best limits



K. Zuber,
Phys. Lett. B 519,1 (2001)

„Solid state TPC“

4 detectors running at LNGS, upgrade to 64 by spring 2005



Sensitivity to right-handed weak currents

- $(A,Z) \rightarrow (A,Z-2) + 2 e^+ (+2\nu_e)$ $\beta+\beta+$
- $e^- + (A,Z) \rightarrow (A,Z-2) + e^+ (+2\nu_e)$ $\beta+/\text{EC}$
- $2 e^- + (A,Z) \rightarrow (A,Z-2) (+2\nu_e)$ EC/EC

Cobra - The people

C. Gößling, H. Kiel, D. Münstermann, S. Oehl, T. Villett
University of Dortmund

T. Leigertwood, D. McKechnan, C. Reeve, J. Wilson, K. Zuber
University of Sussex

P.F. Harrison, Y. Ramachers, D. Stewart
University of Warwick

A. Boston, P. Booth, P. Nolan
University of Liverpool

B. Fulton, R. Wadsworth
University of York

T. Bloxham, M. Freer
University of Birmingham

P. Seller
Rutherford Appleton Laboratory

M. Junker
Laboratori Nazionali del Gran Sasso

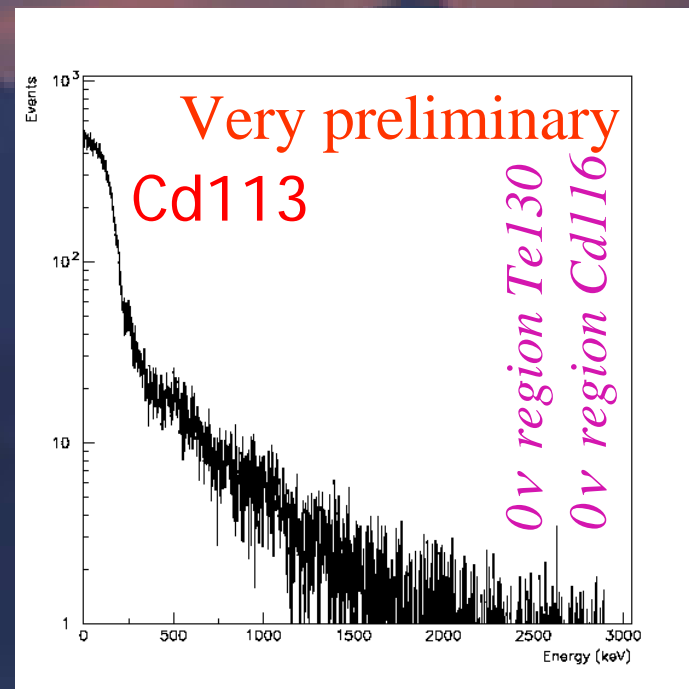
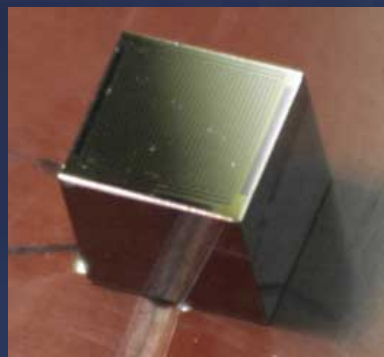
Next step - the 2x2 prototype

Installation of setup at Gran Sasso Underground Laboratory

4 naked 1cm^3 CdZnTe



16. Jan. 2005

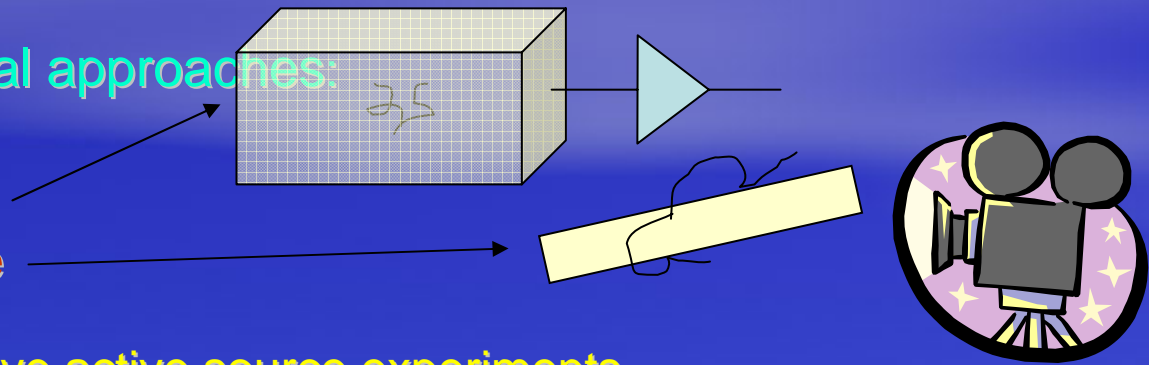


Workshop on beta beams, RAL 1.34 kg x days of data

$0\nu\beta\beta$ Experimental Situation

2 main experimental approaches:

- Active Source
- Passive Source



Best $0\nu 2\beta$ results involve active source experiments

Experiment	Isotope	$T_{1/2}^{0\nu}$ (y)	$\langle m_\nu \rangle$ (eV)
You Ke et al. 1998	^{48}Ca	$> 9.5 \times 10^{21}$ (76%)	< 8.3
Klapdor-Kleingrothaus 2001	^{76}Ge	$> 1.9 \times 10^{25}$	< 0.35
Aalseth et al 2002		$> 1.57 \times 10^{25}$	$< 0.33 - 1.35$
Arnold et al. 2004	^{82}Se	$> 1.3 \times 10^{23}$	$< 1.5-3.1$
Arnold et al. 2004	^{100}Mo	$> 3.1 \times 10^{23}$	$< 0.33-0.84$
Danevich et al. 2000	^{116}Cd	$> 1 \times 10^{23}$	< 2.2
Bernatowicz et al. 1993	$^{130/128}\text{Te}^*$	$(3.52 \pm 0.11) \times 10^{-4}$	$< 1.1 - 1.5$
Bernatowicz et al. 1993	$^{128}\text{Te}^*$	$> 7.7 \times 10^{24}$	$< 1.1 - 1.5$
Arnaboldi et al. 2005	^{130}Te	$> 1.8 \times 10^{24}$	$< 0.5 - 1.1$
Luescher et al. 1998	^{136}Xe	$> 4.4 \times 10^{23}$	$< 1.8 - 5.2$
Belli et al. 2001	^{136}Xe	$> 7 \times 10^{23}$	$< 1.4 - 4.1$
De Silva et al. 1997	^{150}Nd	$> 1.2 \times 10^{21}$	< 3
Danevich et al. 2001	^{160}Gd	$> 1.3 \times 10^{21}$	< 26

18. Jan. 2005

Workshop on beta beams, RAI

Back of the envelope

$$T_{1/2} = \ln 2 \cdot a \cdot N_A \cdot M \cdot t / N_{\beta\beta} \quad (\tau \gg T) \quad (\text{Background free})$$

50 meV implies half-life measurements of 10^{26-27} yrs

1 event/yr you need 10^{26-27} source atoms

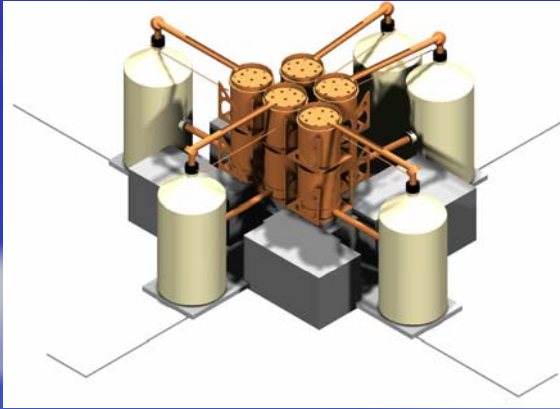
This is about 1000 moles of isotope, implying 100 kg

Now you only can loose: nat. abundance, efficiency, background, ...

Future projects

Experiment	Author	Isotope	Detector description	$T_{1/2}^{5y}$ (y)	$\langle m_{\nu} \rangle^*$
COBRA	Zuber 2001	^{116}Cd	10 kg CdTe semiconductors	1×10^{24}	0.71
CUORICINO	Arnaboldi et al 2001	^{130}Te	40 kg of TeO_2 bolometers	1.5×10^{25}	0.19
NEMO3	Sarazin et al 2000	^{100}Mo	10 kg of bb(0n) isotopes (7 kg Mo) with tracking	4×10^{24}	0.56
CUORE	Arnaboldi et al. 2001	^{130}Te	760 kg of TeO_2 bolometers	7×10^{26}	0.027
EXO	Danevich et al 2000	^{136}Xe	1 t enriched Xe TPC	8×10^{26}	0.052
GEM	Zdesenko et al 2001	^{76}Ge	1 t enriched Ge diodes in liquid nitrogen + water shield	7×10^{27}	0.018
GENIUS	Klapdor-Kleingrothaus et al 2001	^{76}Ge	1 t enriched Ge diodes in liquid nitrogen	1×10^{28}	0.015
MAJORANA	Aalseth et al 2002	^{76}Ge	0.5 t enriched Ge segmented diodes	4×10^{27}	0.025
DCBA	Ishihara et al 2000	^{150}Nd	20 kg enriched Nd layers with tracking	2×10^{25}	0.035
CAMEO	Bellini et al 2001	^{116}Cd	1 t CdWO_4 crystals in liquid scintillator	$> 10^{26}$	0.069
CANDLES	Kishimoto et al	^{48}Ca	several tons of CaF_2 crystal in liquid scintillator	1×10^{26}	
GSO	Danevich 2001	^{160}Gd	2 t $\text{Gd}_2\text{SiO}_5:\text{Ce}$ cristal scintillator in liquid scintillator	2×10^{26}	0.065
MOON	Ejiri et al 2000	^{100}Mo	34 t natural Mo sheets between plastic scintillator	1×10^{27}	0.036
Xe	Caccianiga et al 2001	^{136}Xe	1.56 t of enriched Xe in liquid scintillator	5×10^{26}	0.066
XMASS	Moriyama et al 2001	^{136}Xe	10 t of liquid Xe	3×10^{26}	0.086

Future - Ge approaches



Segmentation and pulse shape discrimination

MAJORANA

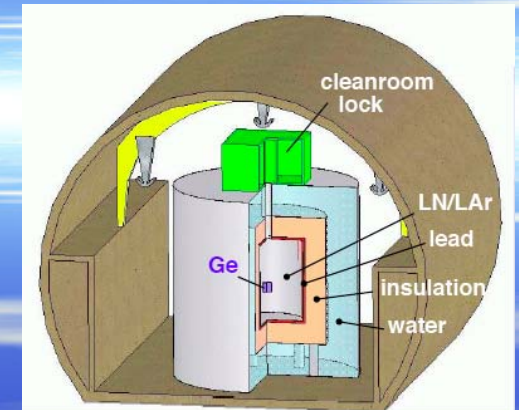
500 kg of enriched Ge detectors



GERDA

Naked enriched Ge-crystals in LAr with lead shield

20 kg enriched Ge-detectors at hand (former HD-MO and IGEX)



MERGE

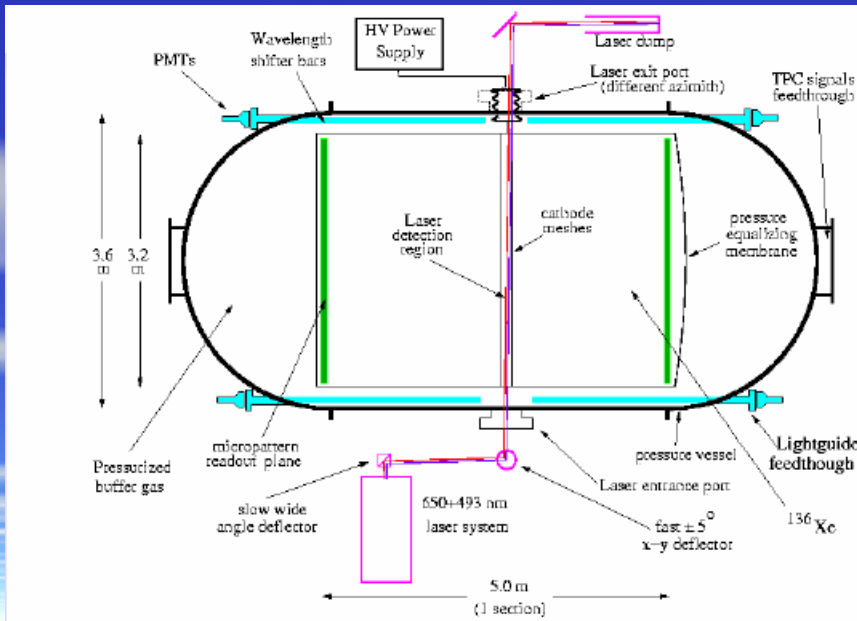
18. Jan. 2005

Workshop on beta beams, RAL



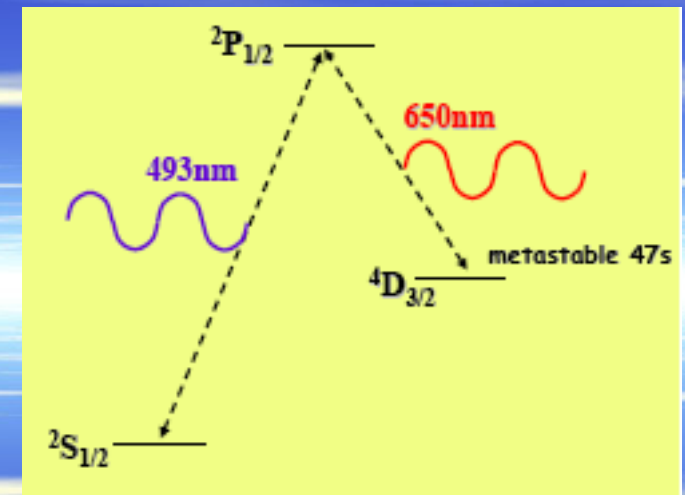
EXO

Tracking and scintillation



New feature:

$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}^{++} e^- e^-$ final state can be identified using optical spectroscopy (M.Moe PRC44 (1991) 931)



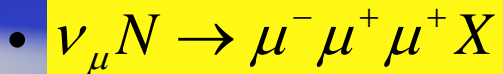
200 kg enriched Xe prototype under construction at WIPP

☞ L=2 processes

In general 9 mass terms

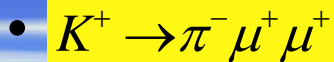
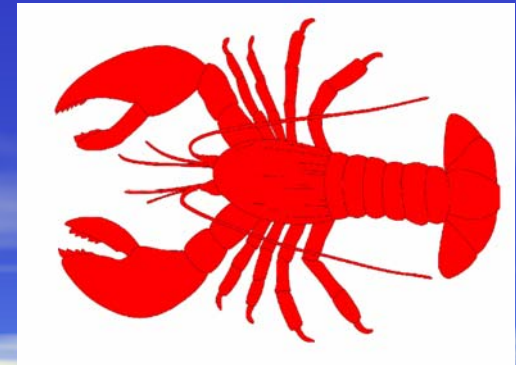
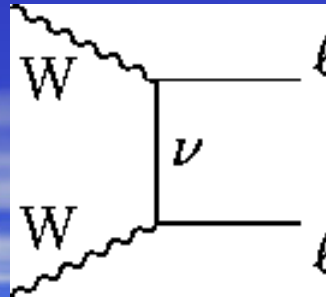
$$\langle m_{\alpha\beta} \rangle = \left| \sum_k U_{\alpha k} U_{\beta k} m_k \right| = \left| \sum_k |U_{\alpha k} U_{\beta k}| m_k \eta_k^{CP} \right|$$

- μe -conversion on nuclei



M. Flanz, W. Rodejohann, K. Zuber,
Eur. Phys. J. C 16, 453 (2001)

W. Rodejohann, K. Zuber,
Phys. Rev. D 63, 054031 (2001)



K. Zuber, Phys. Lett. B 479,33 (2000)



M. Flanz, W. Rodejohann, K. Zuber,
Phys. Lett. B 473, 324 (2000)

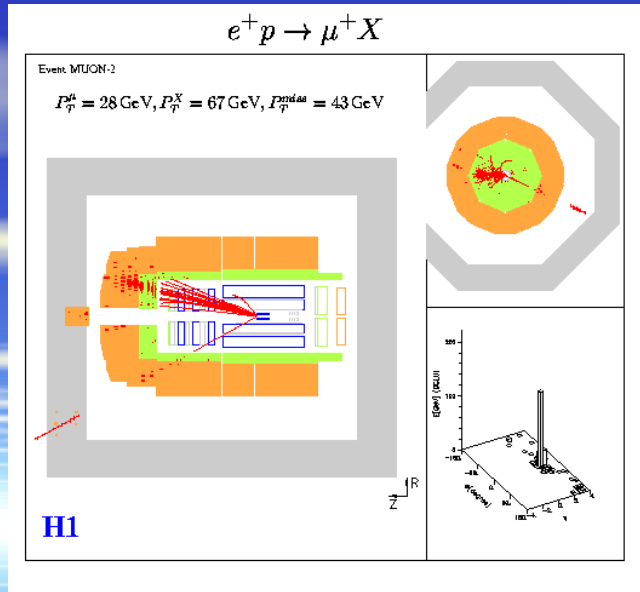
W. Rodejohann, K. Zuber,
Phys. Rev. D 62, 094017 (2000)

limits on $\langle m_{\tau\mu} \rangle$ (in GeV)

$3.5 \cdot 10^{-10}$	$1.7 (8.2) \cdot 10^{-2}$	$8.4 \cdot 10^3$
	500	$8.7 \cdot 10^3$
		$2.0 \cdot 10^4$

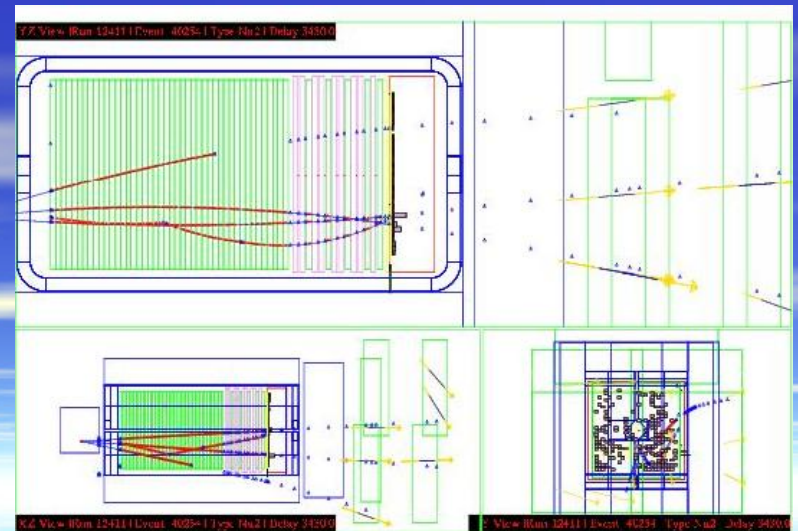
Event candidates

H1 charged current event



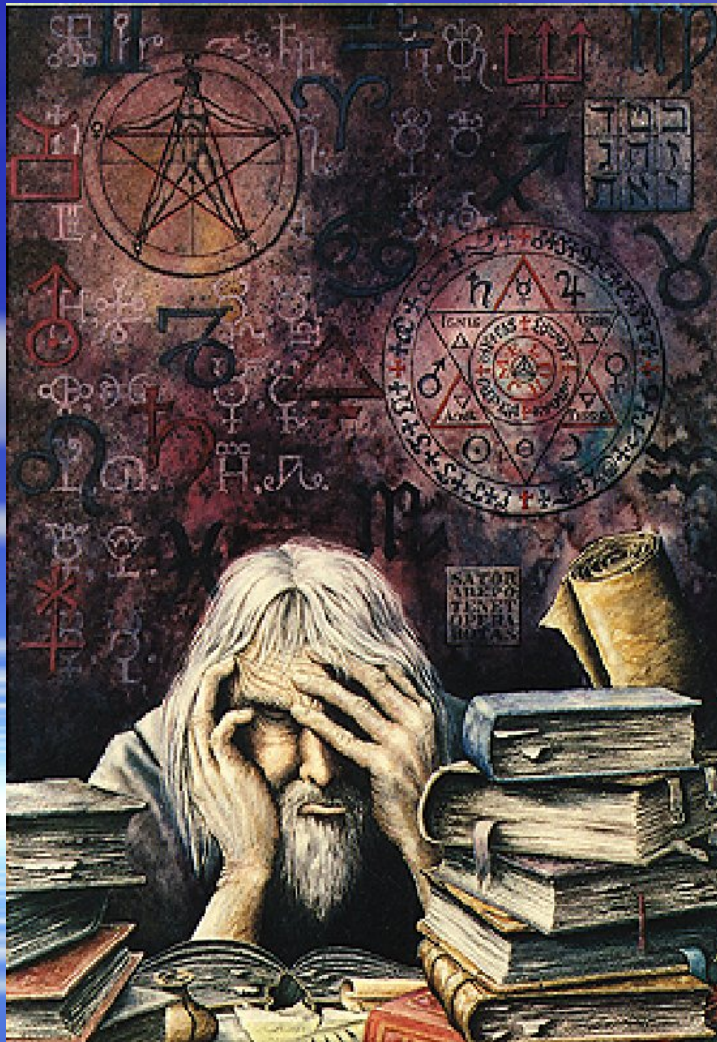
$$e^+p \rightarrow \bar{\nu}_e \mu^+ (\tau^+) \mu^+ (\tau^+) X$$

NOMAD Trimuon event



$$\nu_\mu N \rightarrow \mu^- \mu^+ \mu^+ X$$

Contents



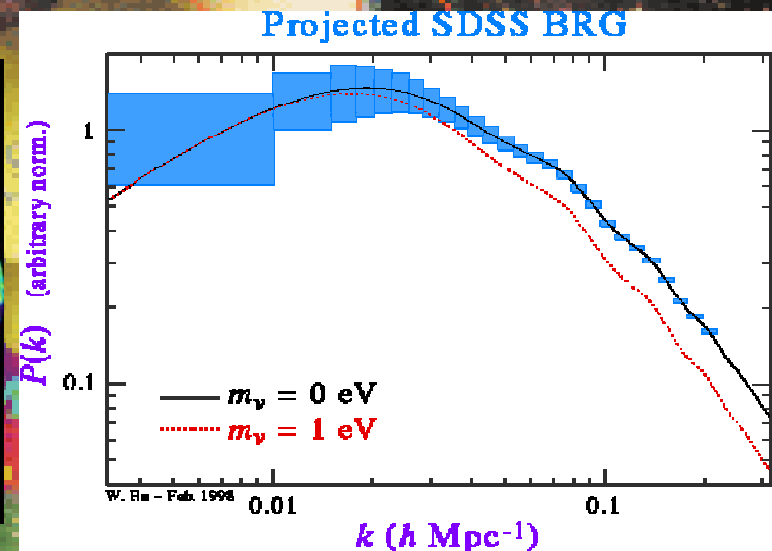
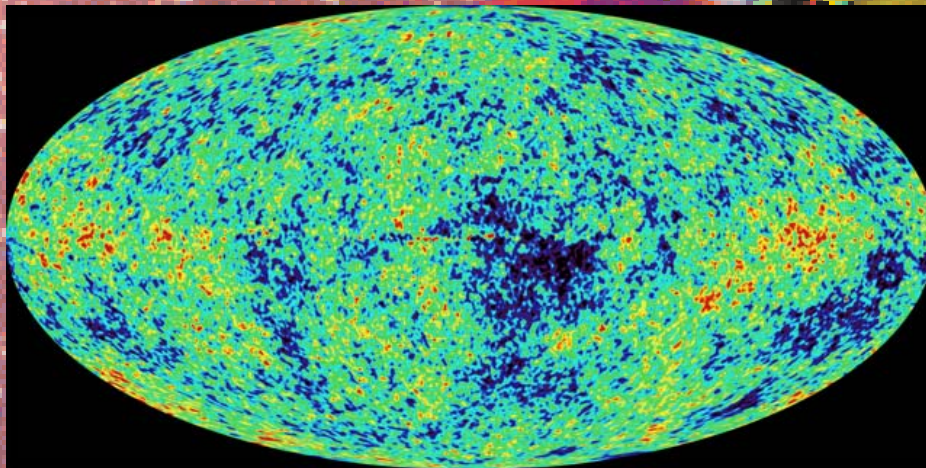
- Beta decay
- Double beta decay
- Cosmological neutrino mass bounds
- Summary and conclusions

Neutrino masses from cosmology

$$n_\nu = \frac{6\zeta(3)}{11\pi^2} T_{CMB}^3 \approx 112 \text{ cm}^{-3}$$

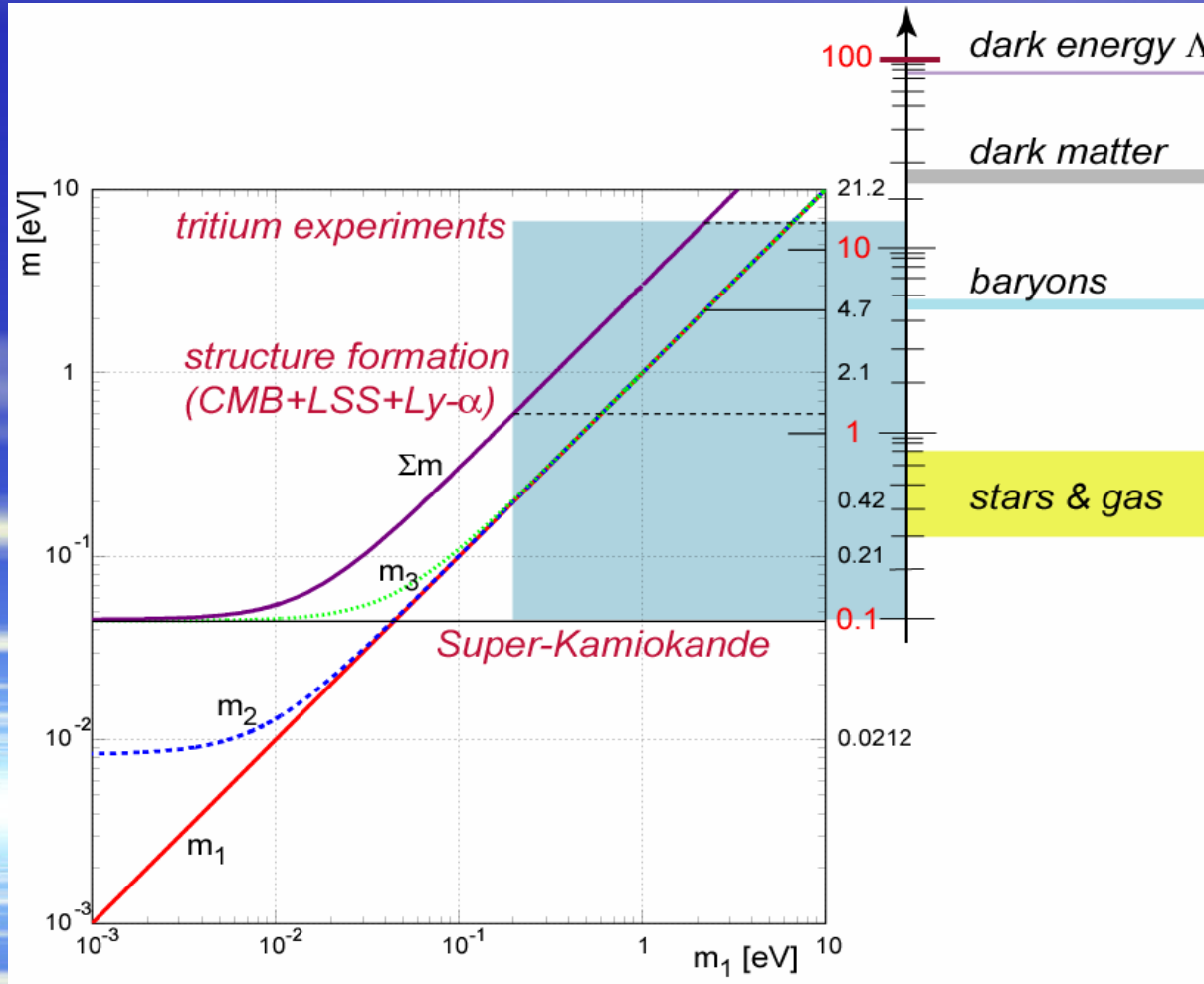
$$\Omega_\nu h^2 = \frac{m_{\nu,tot}}{94 \text{ eV}}$$

New WMAP measurement + SDSS data

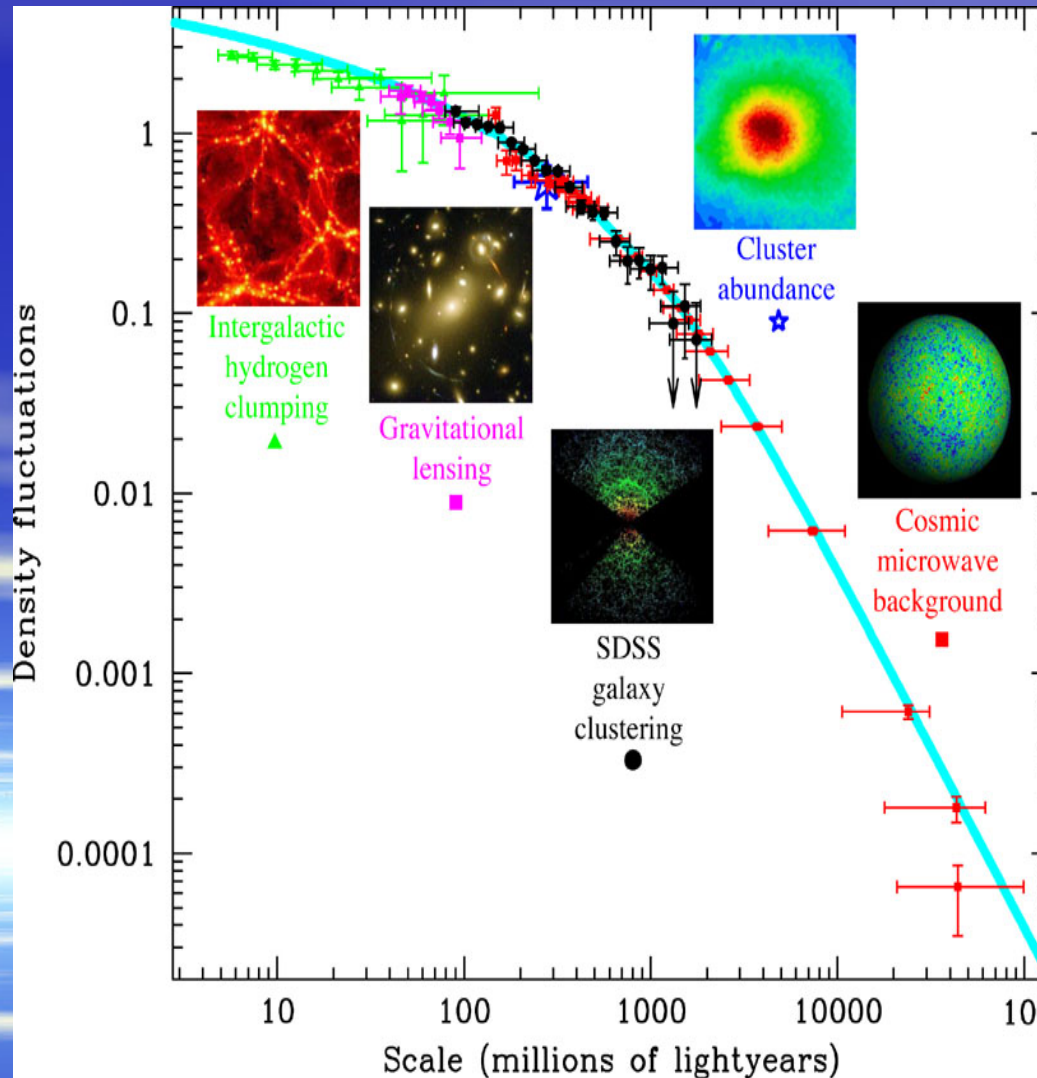


Mass bound model dependent, currently done within Λ CDM

Neutrinos mass density



Density fluctuations versus scale



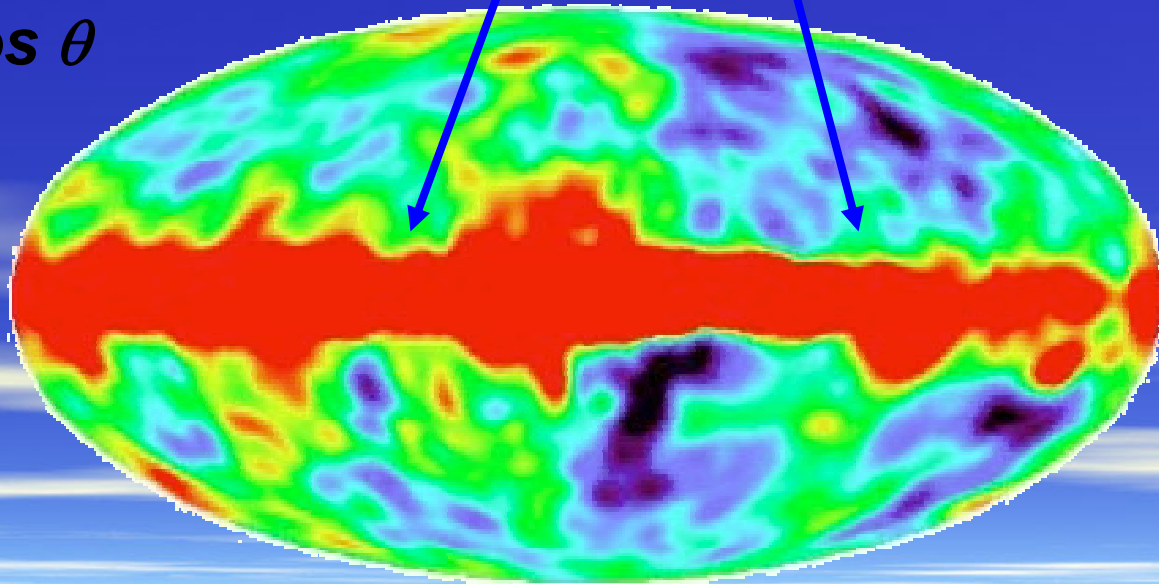
M. Tegmark

(free after Coleridge, 1798)

Structure, structure everywhere

$$C(\theta) = \langle \Delta T(n) \Delta T(n') \rangle$$

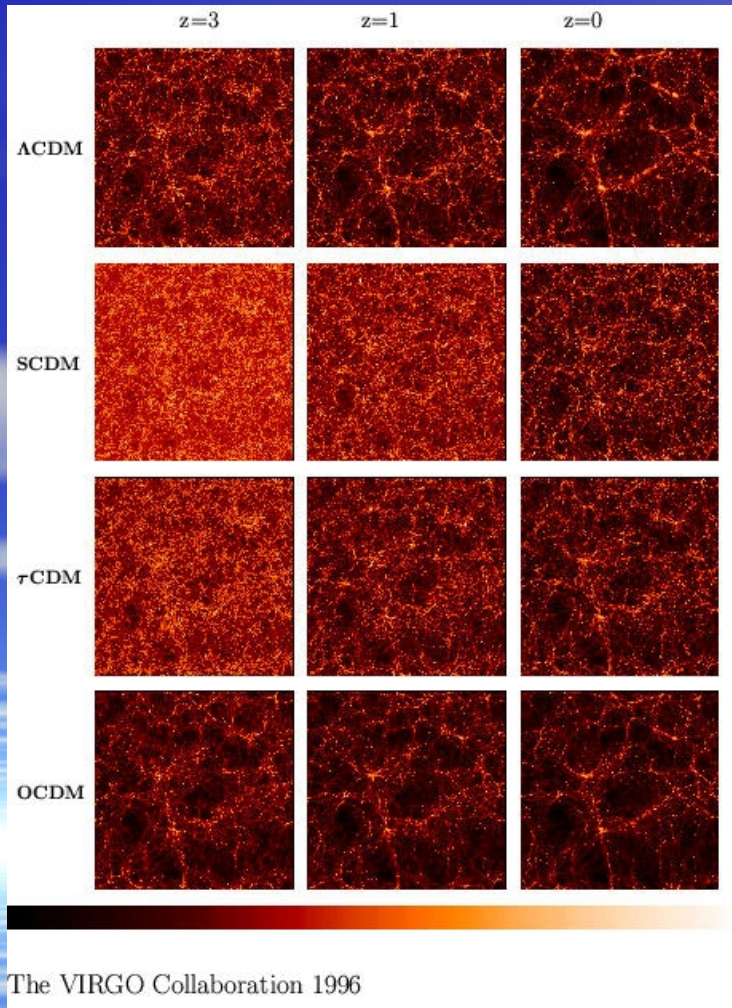
$$\vec{n} \cdot \vec{n}' = \cos \theta$$



Expansion in spherical harmonics

Legendre polynomials

Large scale structure - Description



Measure autocorrelation function

$$\xi(r) = \langle \delta(x)\delta(x+r) \rangle$$

Fourier transformed

$$\xi(r) = \frac{V}{(2\pi)^3} \int |\delta_k|^2 e^{-ikr} d^3k$$

$$\text{Power spectrum } \langle |\delta_k|^2 \rangle \propto k^n$$

Inflation predicts: $n=1$
(Harrison - Zeldovich spectrum)

Neutrinos and the CMB

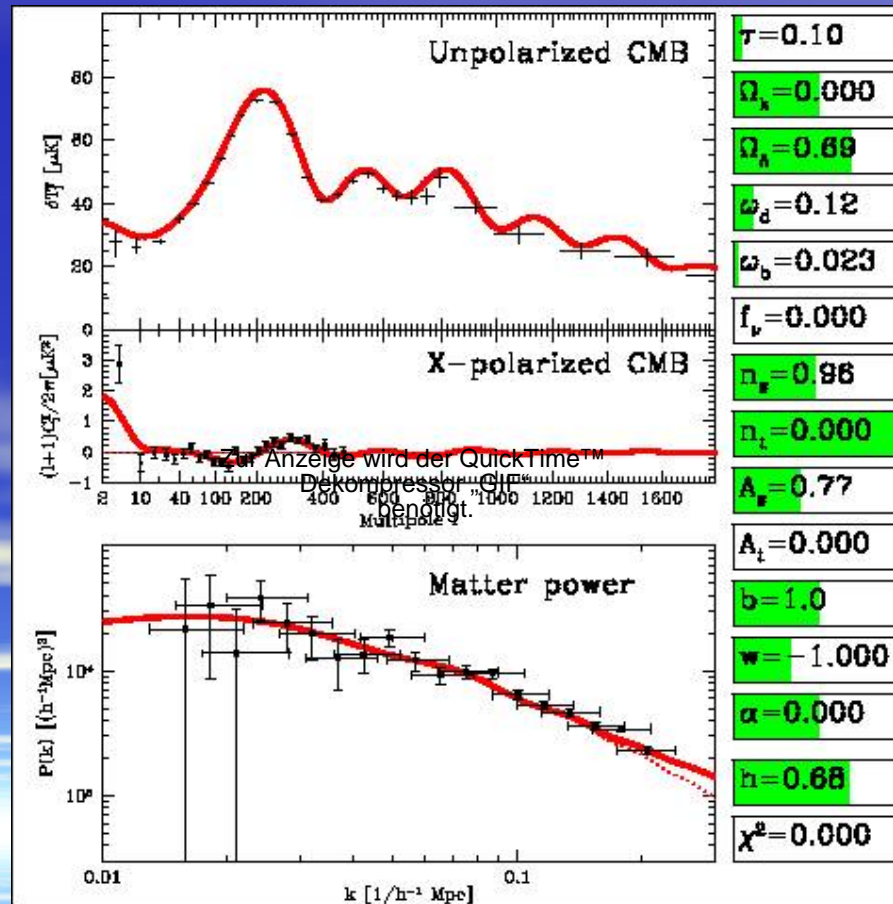
The CMB alone is NOT sensitive to massive neutrinos.

The WMAP result (Spergel et al. 2003) of $m_\nu < 0.69$ eV (95% CL) is based on WMAP+2dF+Ly- α

* 2dF is sensitive to Ω_ν/Ω_m

* WMAP constrains Ω_m (and other parameters)

Neutrinos in cosmology



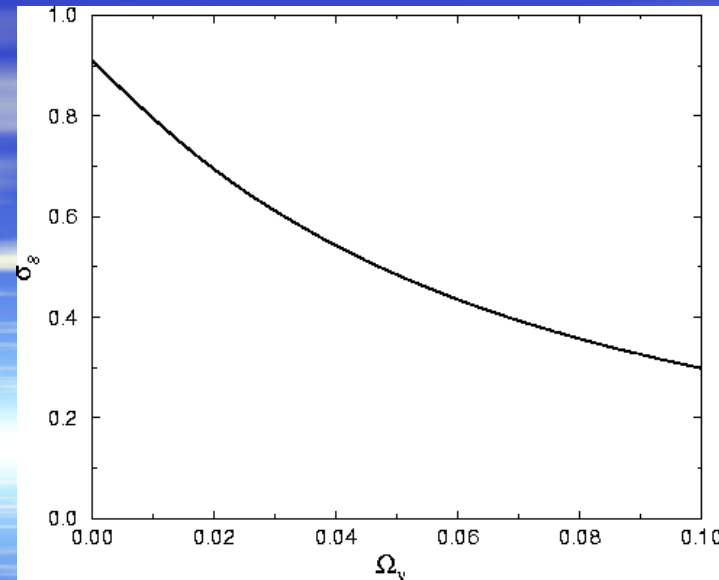
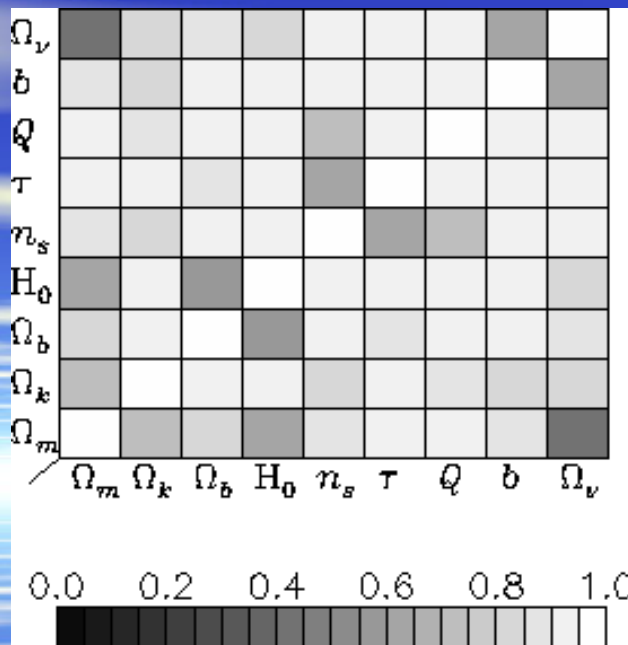
M. Tegmark

CMB and Large scale structure

CMB necessary to fix other cosmological parameters

Neutrinos smear out small density fluctuations, change in power spectrum

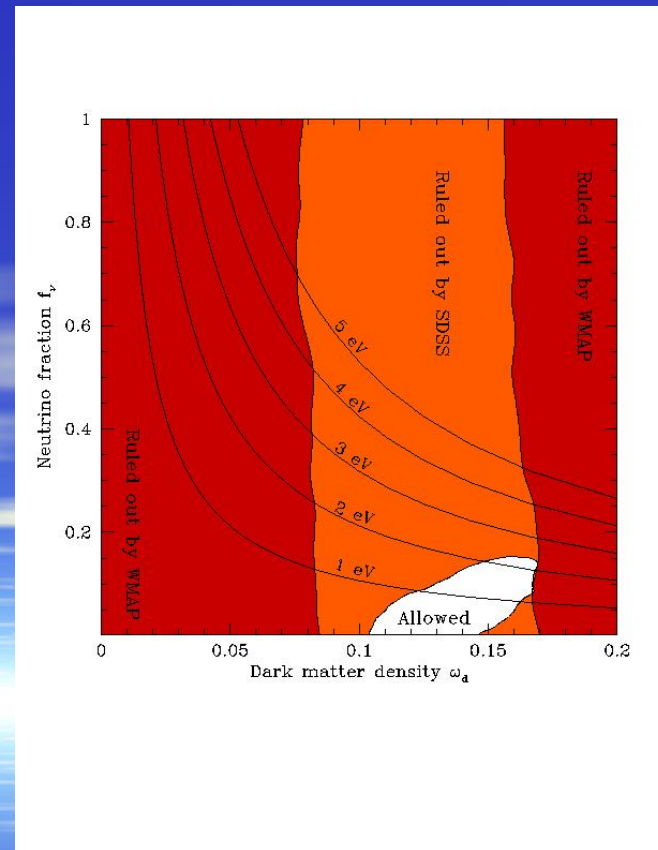
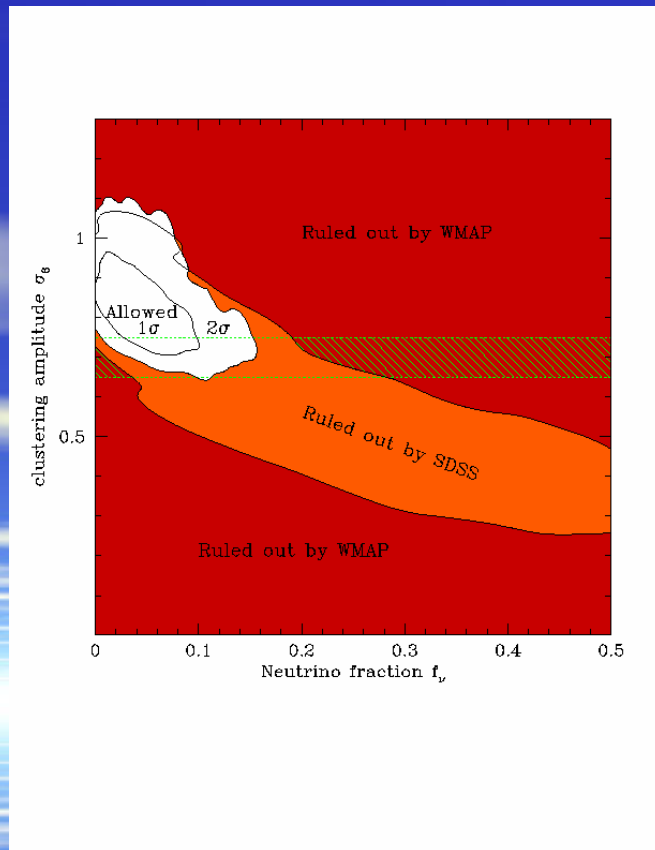
$$\frac{\Delta P_m(k)}{P_m(k)} \approx -8 \frac{\Omega_\nu}{\Omega_m} \quad \text{W. Hu, D. Eisenstein, M. Tegmark, Phys. Rev. Lett. 80, 5255 (1998)}$$



S. Hannestad, Phys. Rev. D 66, 125011 (2002) O.Lahav, O. Elgaroy, astro-ph/0411092

Combined SDSS and WMAP data

M. Tegmark et al., Phys. Rev. D 69, 103501 (2003)



Neutrino mass from cosmology

O. Lahav, Neutrino 2004

Data	Authors	$m_\nu = \Sigma m_i$
2dFGRS	Elgaroy et al. 02	$< 1.8 \text{ eV}$
WMAP+2dF+...	Spergel et al. 03	$< 0.7 \text{ eV}$
WMAP+2dF	Hannestad 03	$< 1.0 \text{ eV}$
SDSS+WMAP	Tegmark et al. 04	$< 1.7 \text{ eV}$
WMAP+2dF+ SDSS	Crotty et al. 04	$< 1.0 \text{ eV}$
Clusters +WMAP	Allen et al. 04	$0.56^{+0.30}_{-0.26} \text{ eV}$

All upper limits 95% CL, but different assumed priors !

Conclusion

Beta decay: Independent of neutrino character

$$\mathbf{m}_e = \sum |U_{ek}|^2 \mathbf{m}_k$$

Double beta decay: Requires Majorana neutrinos

$$\mathbf{m}_{ee} = \left| \sum U_{ek}^2 \mathbf{m}_k \right|$$

Note: U_{PMNS} + 2 Majorana phases

Cosmology: Requires a cosmological model

$$\Omega_\nu h^2 = \frac{m_{\nu, \text{tot}}}{94 \text{ eV}}$$

**Currently all of them give limits around 1 eV,
future very exciting, because large improvements can be
expected**